

# **Autonomous and Mobile Robotics**

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## **Introduction to V-REP with Applications to Motion Planning**

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# outline

- **introduction to V-REP**
  - basic elements
  - dynamic modeling
  - C++ plugins
  - Matlab/Simulink interface
- **applications to task-constrained motion planning**
  - with **moving obstacles**
  - in the presence of **soft task constraints**
  - for **humanoid robots**

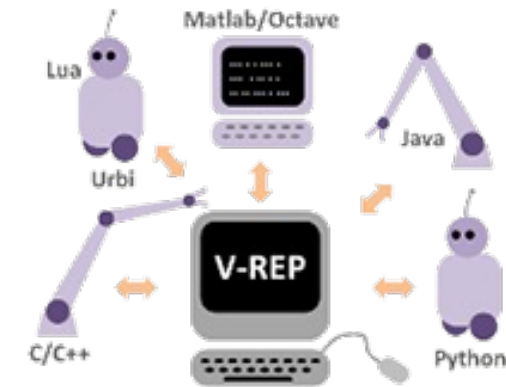
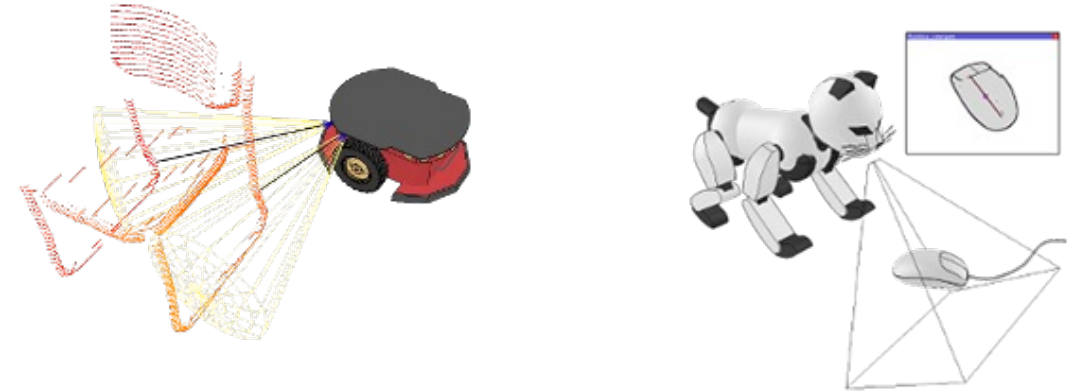
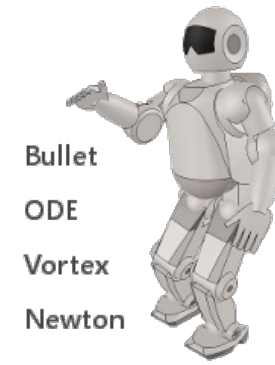
# the V-REP simulator

- V-REP = **Virtual Robot Experimentation Platform**
- a robotic simulator: a software environment aimed at generic robotic applications (not only motion planning)
- relatively new (2014), produced by Coppelia Robotics
- **free** and **open source**
- available on Windows, Linux and Mac
- **example of applications**
  - fast prototyping and verification
  - fast algorithm development
  - hardware control
  - etc



# the V-REP simulator

- provides physical engines for **dynamic simulations**
- allows the simulation of **sensors**
- its functionalities can be easily extended using **many programming languages** (C/C++, Python, Java, Lua, MATLAB, Octave, Urbi) and **programming approaches** (remote clients, plugins, ROS nodes,...)
- provides a large and continuously growing **library of robot models**



# three central elements

how to **build**  
a robot

Scene  
Objects

Calculation  
Modules

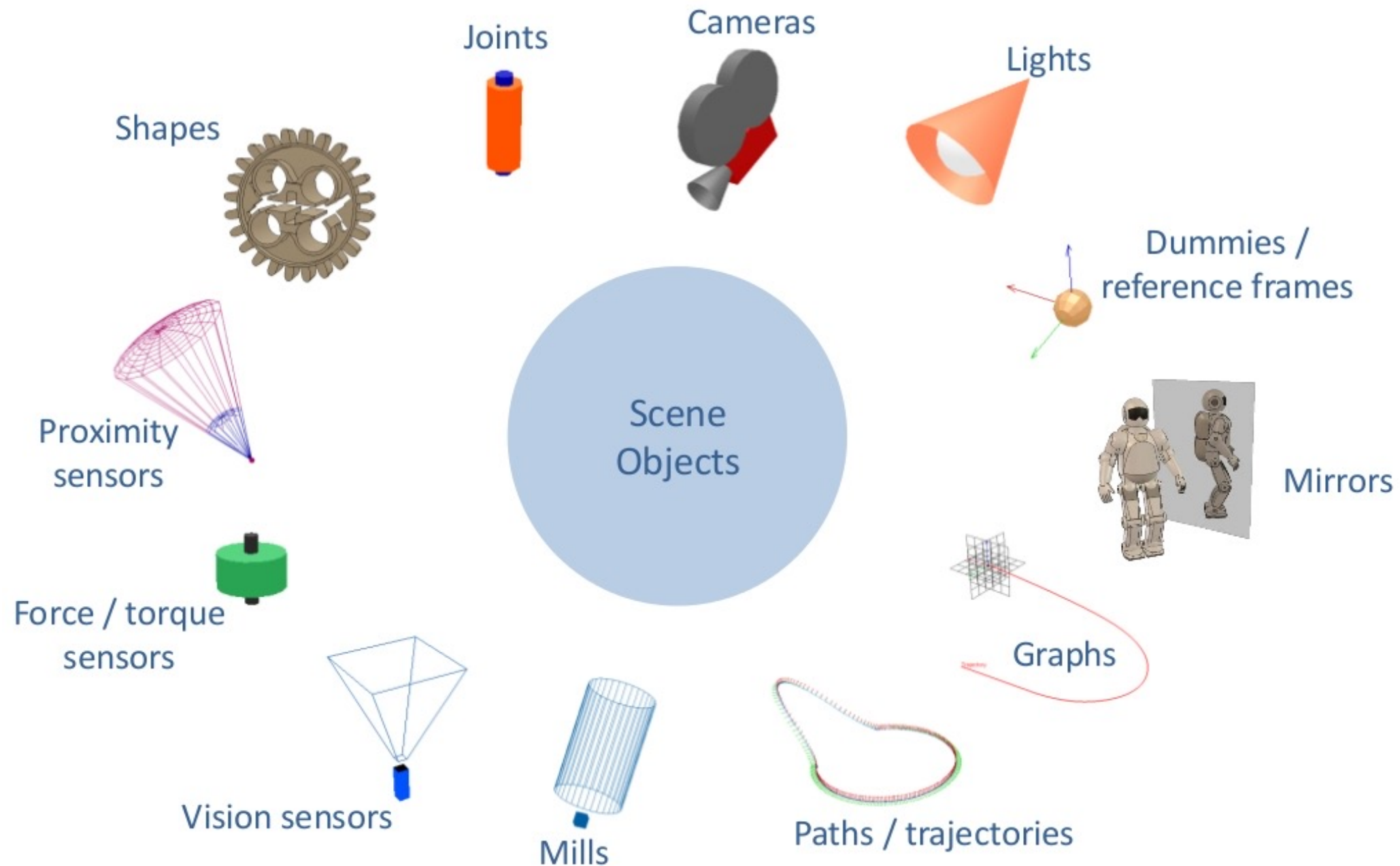
how to **simulate**  
a robot

Control  
Mechanisms

how to **control**  
a robot

# scene objects

- how to **build** a robot



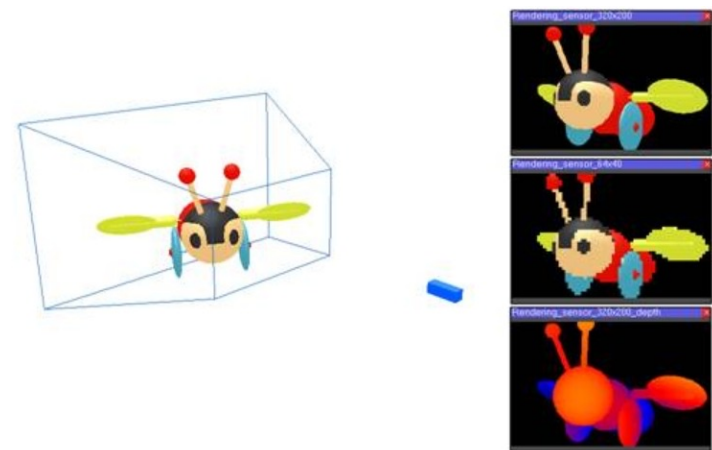
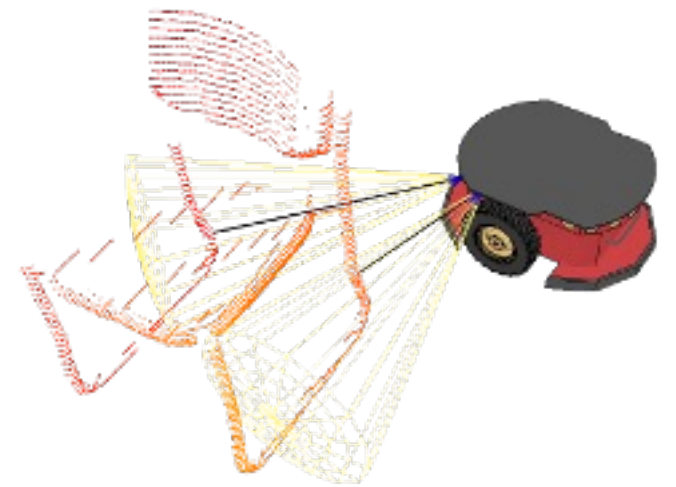
# scene objects: basic components

- **shapes**
  - rigid mesh objects that are composed of triangular faces
  - can be grouped/ungrouped
  - different types (random, convex, pure shapes)
- **joints**
  - revolute: rotational movement
  - prismatic: translational movement
  - screw: translational while rotational movement
  - spherical: three rotational movements
- a **robot model** can be created through a **hierarchical structure** including (at least) shapes and joints



# scene objects: sensors

- **proximity sensors**
  - more than simple ray-type detection
  - configurable detection volume
  - fast minimum distance calculation within volume
- **vision sensors**
  - render the objects that are in their field of view
  - embedded image processing
  - two different types: orthographic projection-type (e.g., close-range infrared or laser range finders) and perspective projection-type (e.g., camera-like sensors)
- **torque/force sensors**
  - measure applied force/torque (on 3 principal axes)

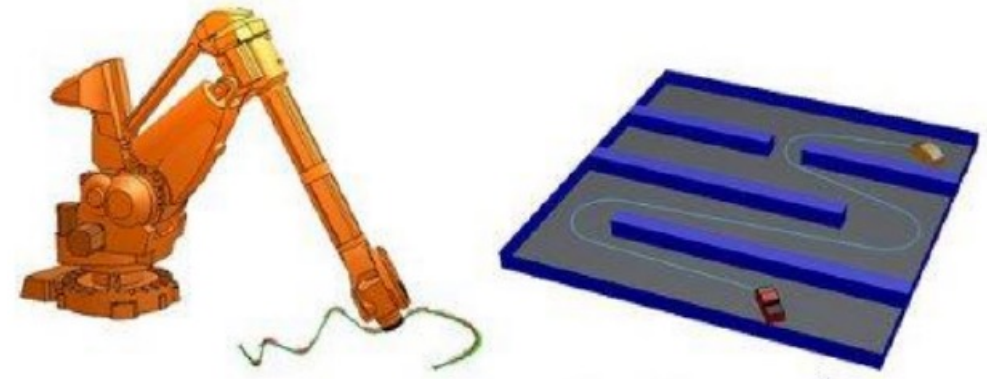




# scene objects: other components

- **paths/trajectories**

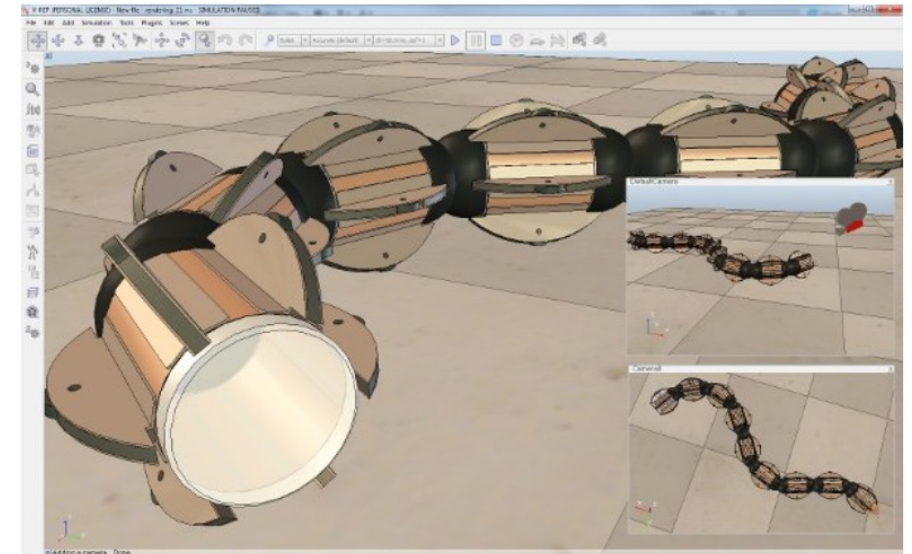
- allow 6D definitions
- can be easily created  
(by importing a file or defining control points)



- **cameras**

- perspective/orthographic projection
- can track an object while moving

- **lights**: omnidirectional, spotlight, directional



- **mirrors**: reflect images/light, auxiliary clipping frame

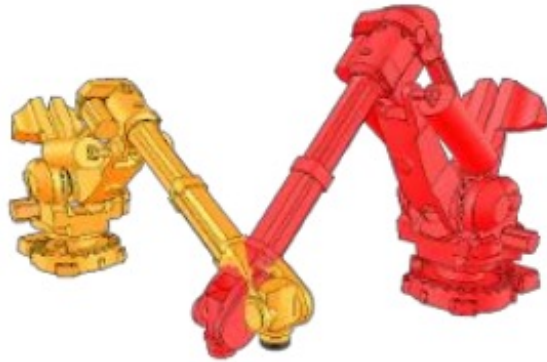
- **graphs**: draw 3D curves, easily exportable

- **dummies**: auxiliary reference frame

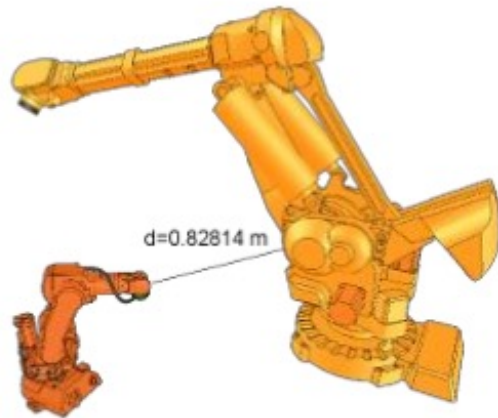


# calculation modules

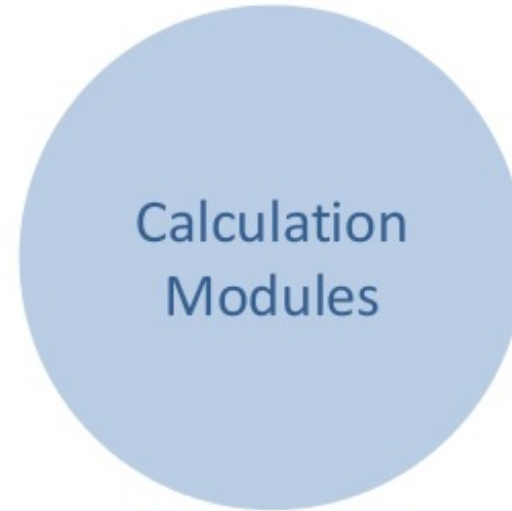
- how to **simulate** a robot



Collision detection



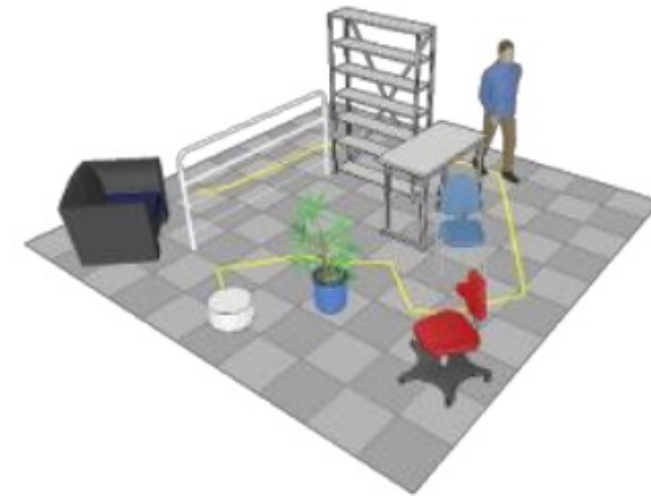
Minimum distance calculation



Calculation  
Modules



Physics / Dynamics



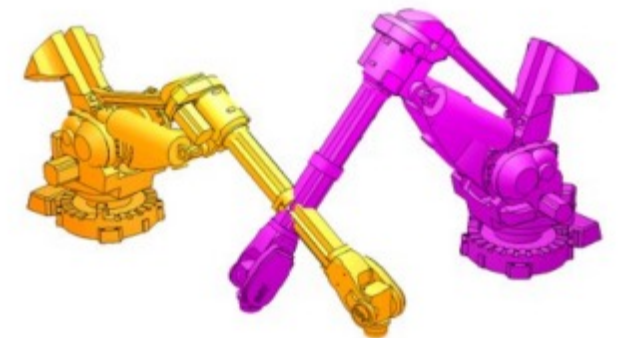
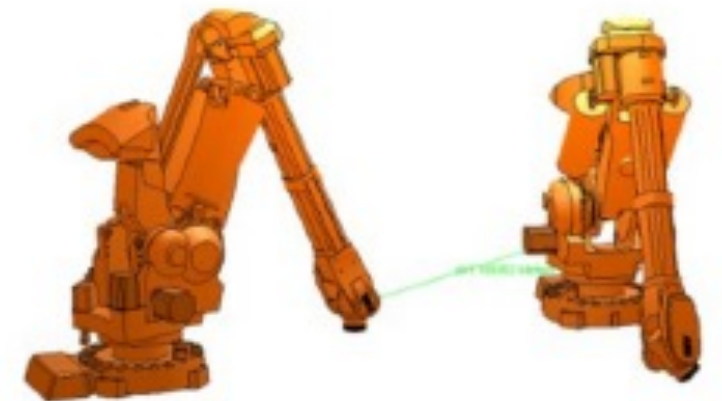
Path / motion planning



Forward / Inverse kinematics

# calculation modules

- **forward/inverse kinematics**
  - can be used for any kinematic chain (closed, redundant, ...)
  - build inverse kinematic (IK) group
  - different techniques for inverse kinematics (pseudoinverse, damped least square)
  - accounts for joint limits and obstacle avoidance
- **minimum distance computation**
  - can be used between any pair of meshes
  - very fast and optimized
- **collision detection**
  - can be used between any pair of meshes
  - scene objects can be defined as collidable or not

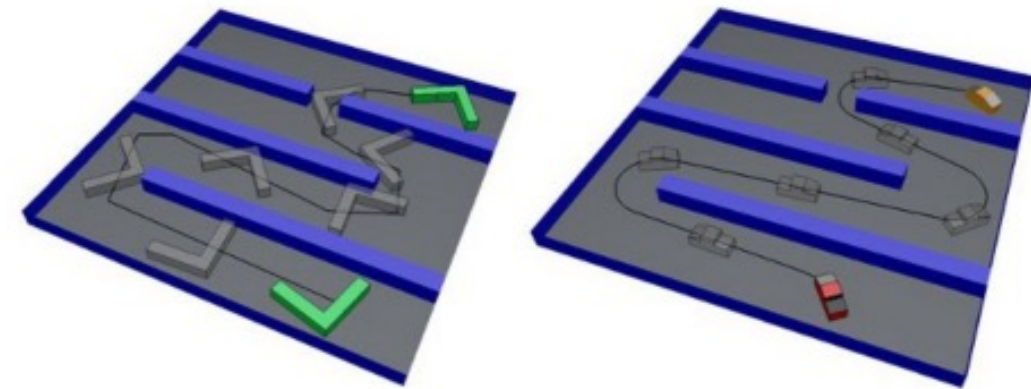




# calculation modules

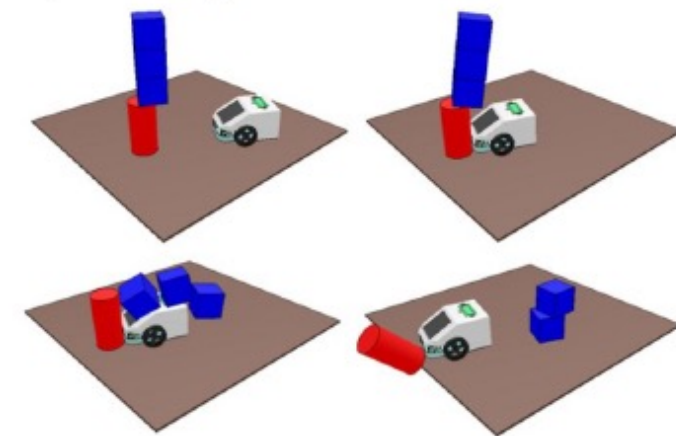
- **path/motion planning**

- can be performed for any kinematic chain
- holonomic/non holonomic path planning
- requires the specification of: start/goal configuration, obstacles, robot model
- uses the OMPL library



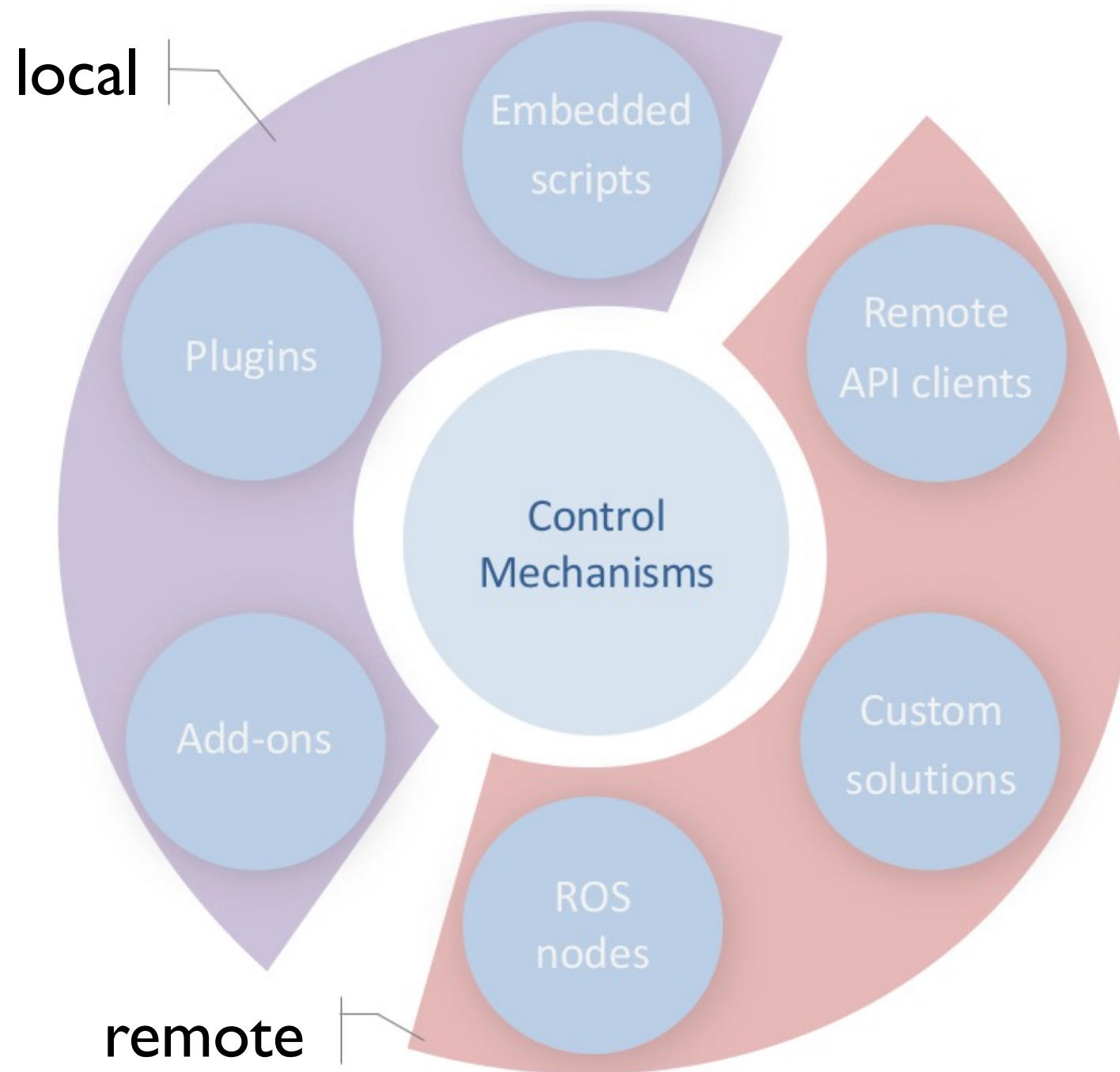
- **physics/dynamics**

- enable dynamic simulations (gravity, friction, ...)
- four different physical engines: Bullet, ODE, Vortex, Newton (ordered by computational demand)
- dynamic particles to simulate air or water jets



# control mechanisms

- how to **control** a robot

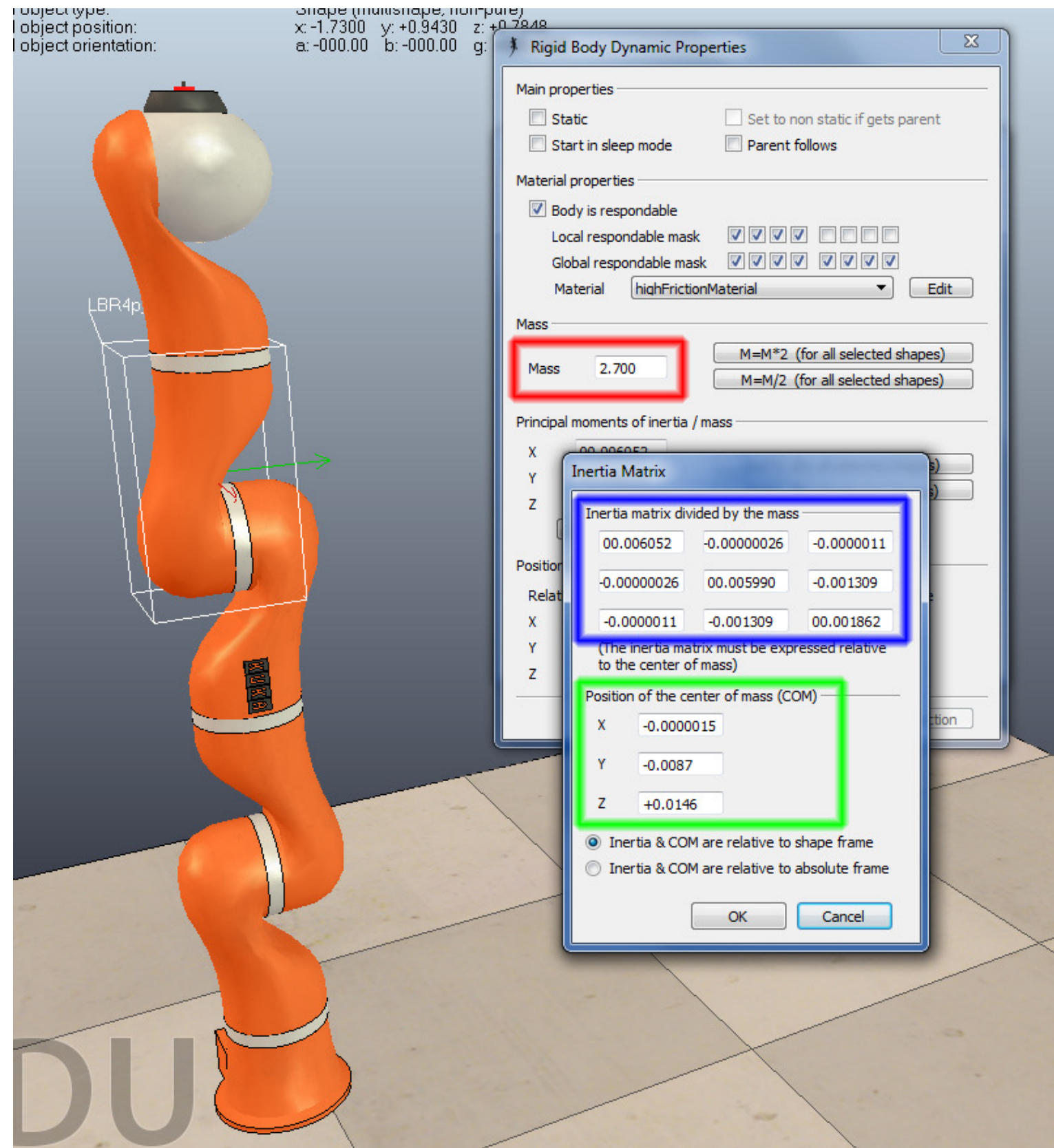


# control mechanisms

- **local** approach: control entity is internal
  - embedded script: associated to a single robot
  - add-on: can only execute minimalistic code
  - **plugin**: most general tool, fast computation, written in C++
- **remote** approach: control entity is external
  - ROS node: bridge between V-REP and ROS
  - custom solution: client/server paradigm using the BlueZero framework
  - **remote API client**: communication between VREP and an external application (e.g., Matlab/Simulink)

# dynamic modeling of a robot

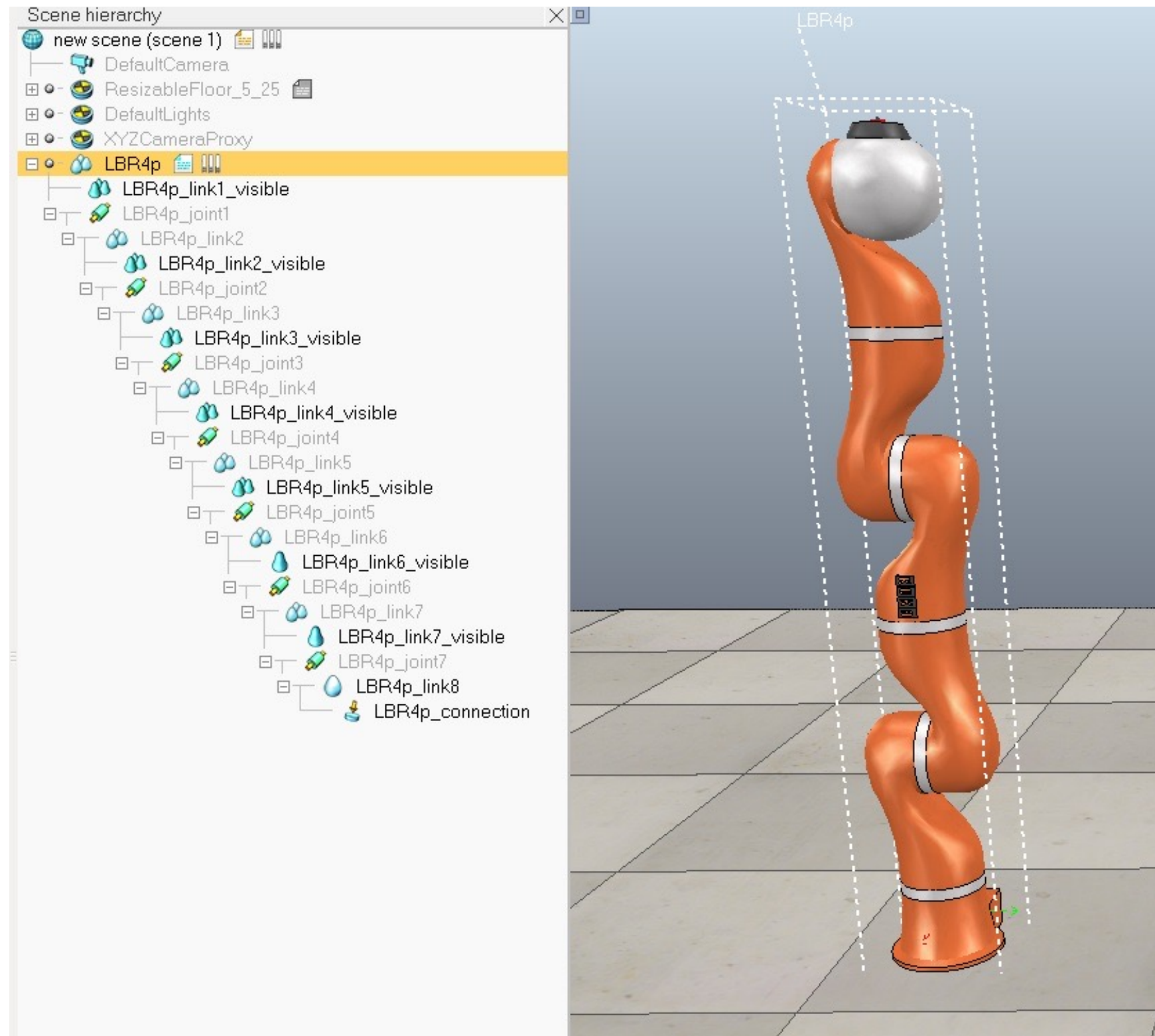
- building a **dynamic model** in V-REP is very easy: no equations are needed
- it requires a few simple steps:
  1. import a **CAD model** of the robot
  2. associate to each body of the robot its **dynamic parameters**: mass, center of mass, inertia matrix





# dynamic modeling of a robot

3. build a **model tree**:  
a tree that represents all hierarchical information of the kinematic chains (links and joints)



# C++ plugins

- uses the **V-REP regular APIs** (more than 450 functions available)
- produces a **shared library** (e.g., **.so** for Linux and **.dll** for Windows)
- automatically loaded by V-REP at program start-up
- can be integrated with other **C++ libraries** (e.g., Eigen, Octomap, etc)
- two main applications
  - extend V-REP's functionality through **user-written functions** (e.g., motion planning algorithms, controllers, ...)
  - used as a **wrapper** for running code written in other languages
- a single plugin can manage **more than one robot**
- fast execution (particularly suited for motion planning)

# C++ plugins

- at each **event** in the V-REP interface, a corresponding message is sent to the plugin
- each **message** triggers the execution of a particular portion of the code in the plugin

before starting the simulation (“**offline**” functions)

simulation  
is stopped

```
if (message == sim_message_eventcallback_simulationabouttostart) { // Simulation is about to start
    Planning();
}

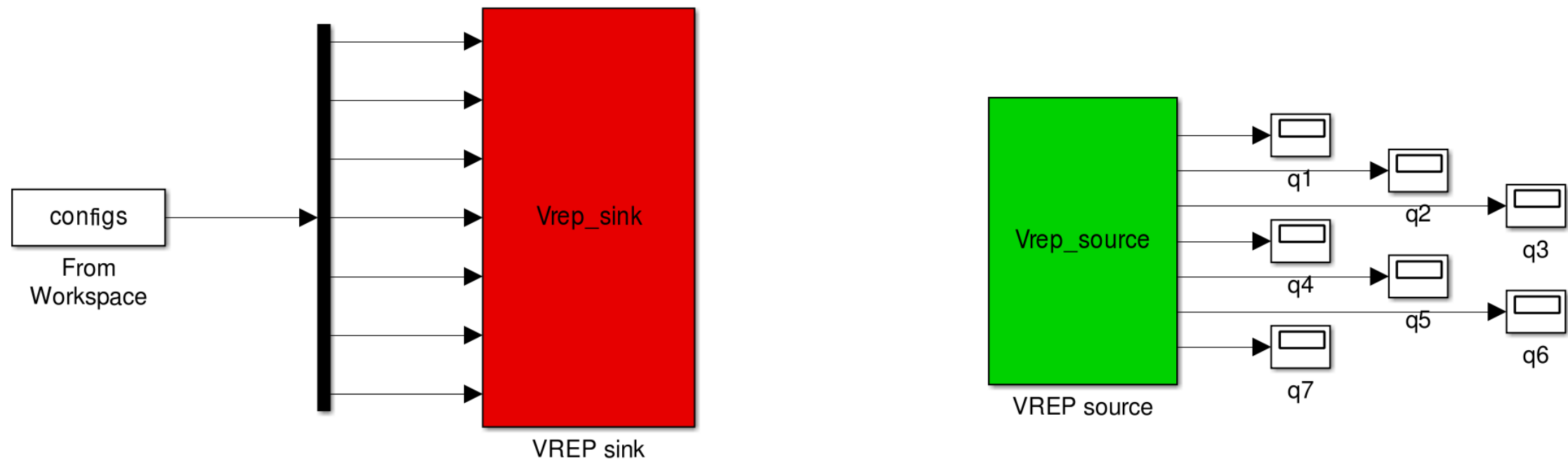
if (message == sim_message_eventcallback_simulationended) { // Simulation just ended
    std::cout << "Simulation Concluded" << std::endl;
}

if (message == sim_message_eventcallback_modulehandle) { // Simulation is running
    Execution();
}
```

during the simulation (“**online**” functions)

# Matlab/Simulink interface

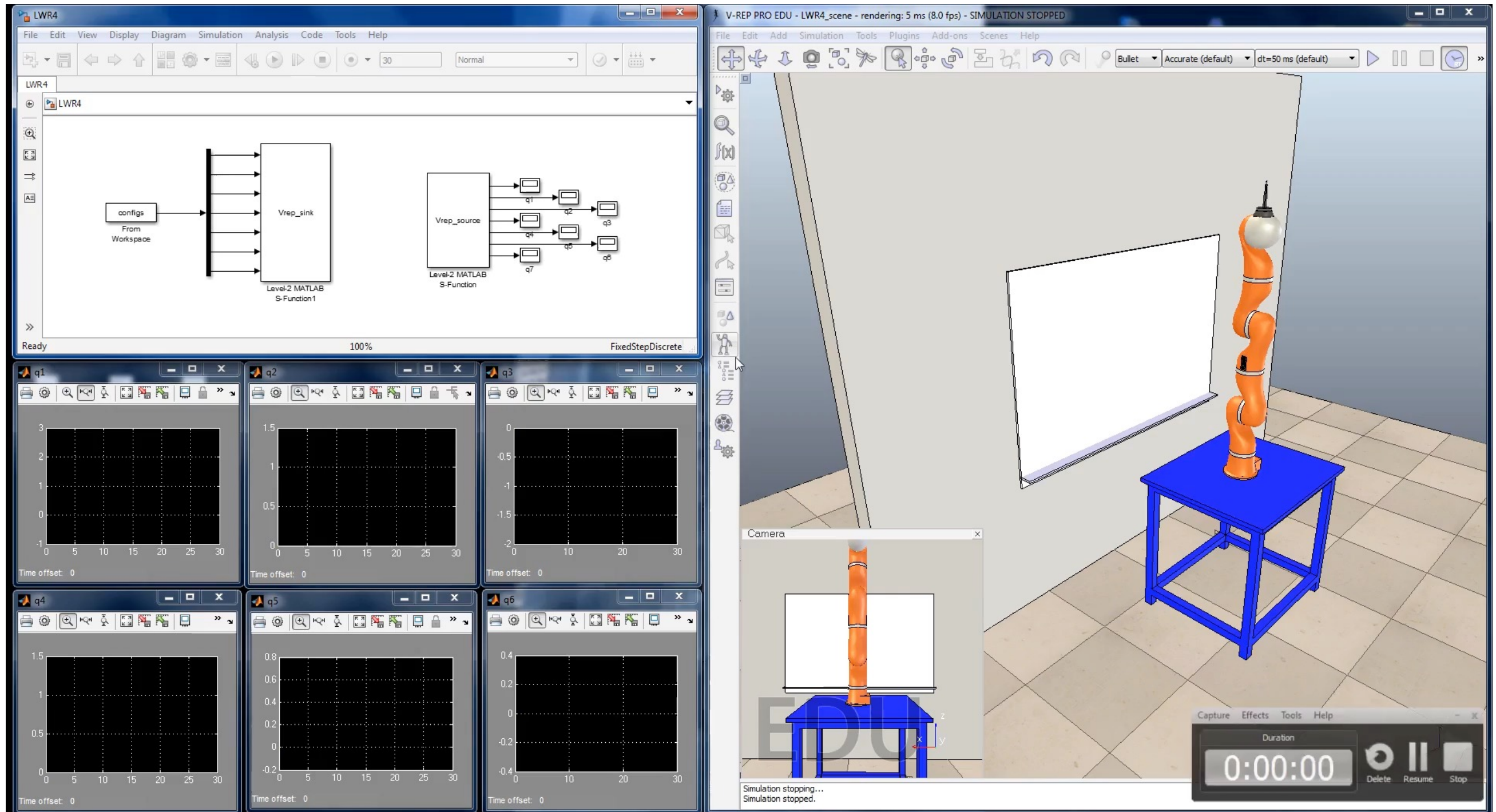
- uses the **V-REP remote APIs** (more than 100 functions available)
- an interface for sending/receiving commands to/from V-REP
- two main blocks: **V-REP sink** and **V-REP source** respectively sends/reads values from V-REP joints



- V-REP and Matlab/Simulink times automatically synchronized
- Matlab/Simulink commands start/stop V-REP simulations



# Matlab/Simulink interface

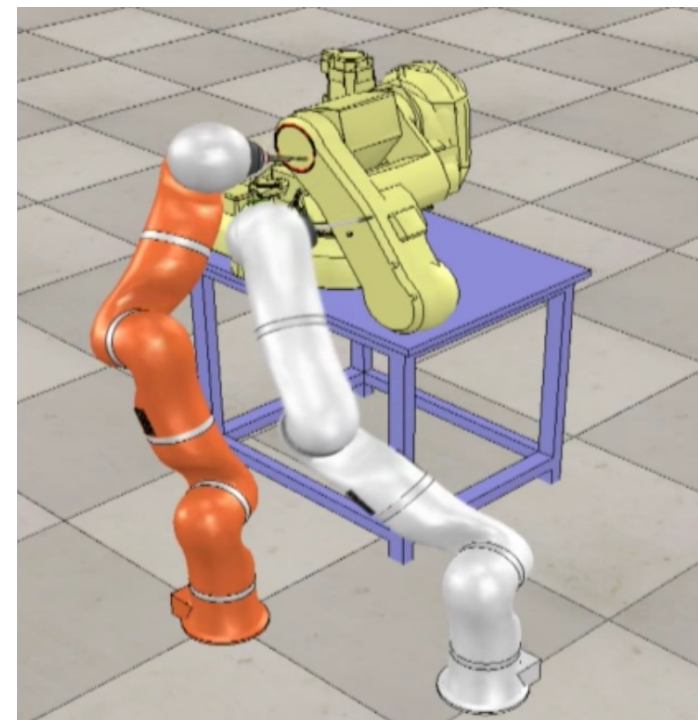


## wrap up

- V-REP **main advantages**
  - very good online documentation
  - four different **physics engines**
  - most complete open source software for dynamic simulations
  - very good set of APIs and control mechanisms
  - very fast software development when one gets the V-REP structure
- V-REP **main drawbacks**
  - vision sensors have high computational payload
  - since it is a huge software, it is not so friendly at the beginning
  - multi-robot simulations have high computational payload
  - **collision checking** library is slow

# task-constrained motion planning with moving obstacles (TCMP-MO)

- **problem**: find **feasible**, **collision-free** motions for a robot that is assigned a **task constraint** in an environment containing **moving obstacles**
- the robot **configuration**  $q$  takes values in a  $n_q$ -dimensional configuration space
- the **task** is defined by a **desired task path**  $y_d(s)$ ,  $s \in [0,1]$ , that takes values in an  $n_y$ -dimensional task space
- **assumptions**
  - the robot is **kinematically redundant** w.r.t. the task ( $n_q > n_y$ )
  - the obstacle trajectories are **known**

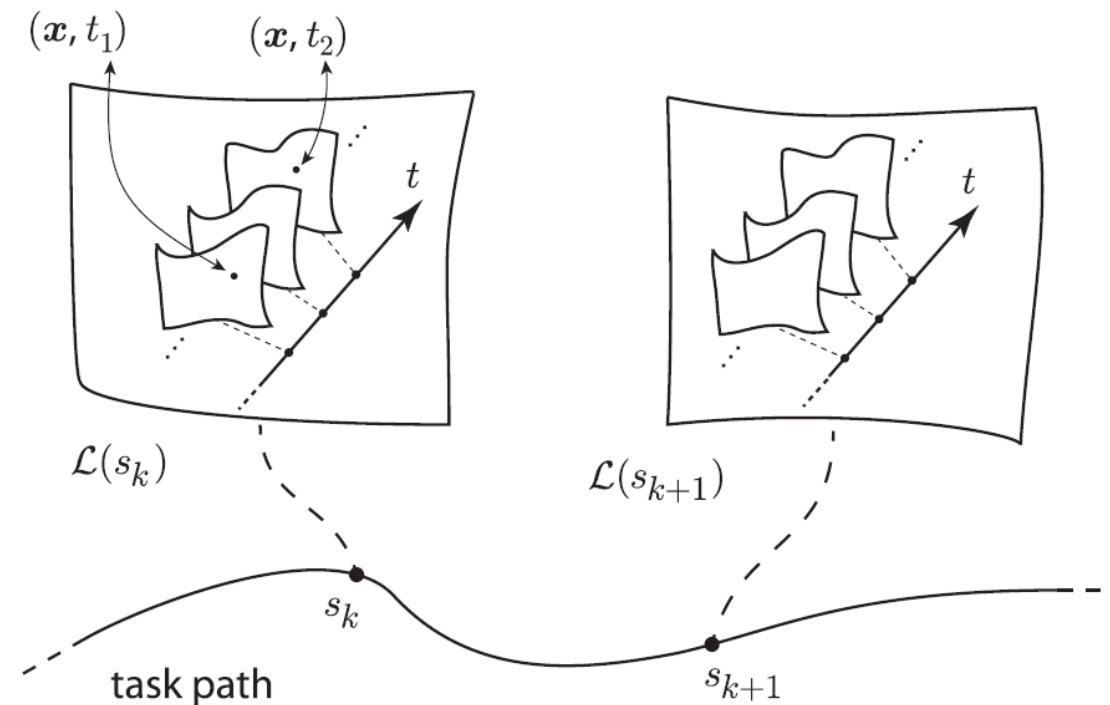




# TCMP-MO

- in the **kinematic case**  
robot described by the **kinematic-level model**  $\dot{q} = v$   
with generalized velocities  $\dot{q} = \dot{s}q'$ , and state  $x = q$
- in the **dynamic case**  
robot described in the **Euler-Lagrange form**  $B(q)\ddot{q} + n(q, \dot{q}) = \tau$   
with generalized accelerations  $\ddot{q} = \dot{s}^2 q'' + \ddot{s}q'$ , and state  $x = (q, \dot{q})$
- **solution** to the TCMP-MO problem: a **configuration-space trajectory**  $q(t)$ , i.e., a **path**  $q(s)$  + a **time history**  $s(t)$ , such that:
  - the assigned task path is continuously satisfied
  - collisions are always avoided
  - joint velocity limits (kinematic case) or joint velocity/torque limits (dynamic case) are respected

# search space



- in general, a state may be admissible at a certain time instant and not admissible at another due to the movements of the obstacles
- **task-constrained state-time space (STS)**  $\mathcal{S}_{\text{task}}$  decomposes as a **foliation**, i.e.,  $\mathcal{S}_{\text{task}} = \bigcup_{s \in [0,1]} \mathcal{L}(s)$  with  $\mathcal{L}(s)$  the generic **leaf**

– in the **kinematic case**

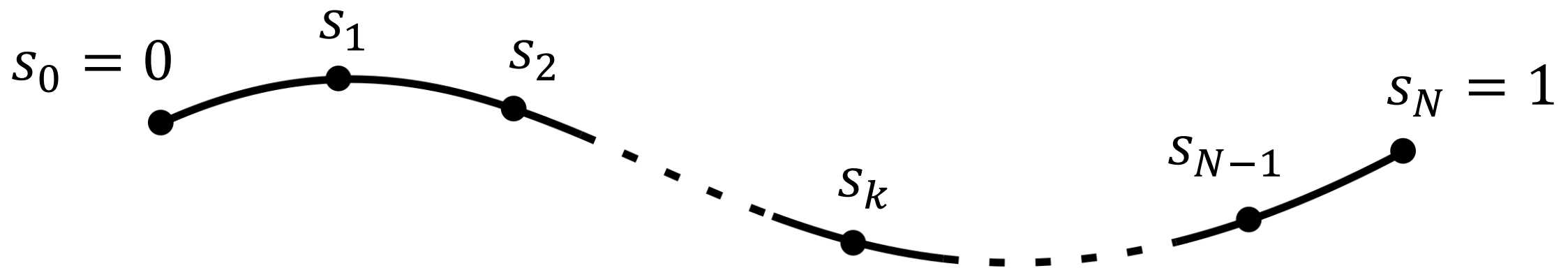
$$\mathcal{L}(s) = \{(\mathbf{q}, t) \in STS: \mathbf{f}(\mathbf{q}) = \mathbf{y}_d(s)\}$$

– in the **dynamic case**

$$\mathcal{L}(s) = \{(\mathbf{q}, \dot{\mathbf{q}}, t) \in STS: \mathbf{f}(\mathbf{q}) = \mathbf{y}_d(s), J(\mathbf{q})\dot{\mathbf{q}} = \dot{\mathbf{y}}'_d(s)\}$$

# approach

- an **offline randomized algorithm**
- builds a **tree**, similarly to the RRT, in  $\mathcal{S}_{\text{task}} \cap \mathcal{S}_{\text{free}}$ 
  - a **vertex** contains a **state** of the robot and an associated **time instant**
  - an **edge** between two adjacent vertexes represents a feasible collision-free **subtrajectory** in the configuration space
- makes use of  $N + 1$  **samples** of the desired task path  $\mathbf{y}_d(s)$ , corresponding to the **equispaced sequence**  $\{s_0 = 0, s_1, \dots, s_N = 1\}$



## the kinematic case

- root the tree at  $(\mathbf{q}_{ini}, 0)$
- iteratively
  - randomly select a **sample**  $\mathbf{y}_{rand}$
  - compute an **IK solution**  $\mathbf{q}_{rand} = \mathbf{f}^{-1}(\mathbf{y}_{rand})$
  - randomly assign to  $\mathbf{q}_{rand}$  a time instant  $t_{rand}$
  - search the **closest vertex**  $(\mathbf{q}_{near}, t_{near})$  to  $(\mathbf{q}_{rand}, t_{rand})$ , and extract  $s_k$  associated to  $\mathbf{q}_{near}$
  - generate **forward/backward motions**
    - **time histories**: randomly choose two values of  $\dot{s}$  (pos/neg)
    - **subpaths**: numerically integrate using random  $\tilde{\mathbf{w}}$ 
$$\mathbf{q}' = \mathbf{J}^\# (\pm \mathbf{y}'_d + k_p \mathbf{e}_y) + (\mathbf{I} - \mathbf{J}^\# \mathbf{J}) \tilde{\mathbf{w}}$$
  - if **no violation** occurs, add new vertices and edges to the tree

## the dynamic case

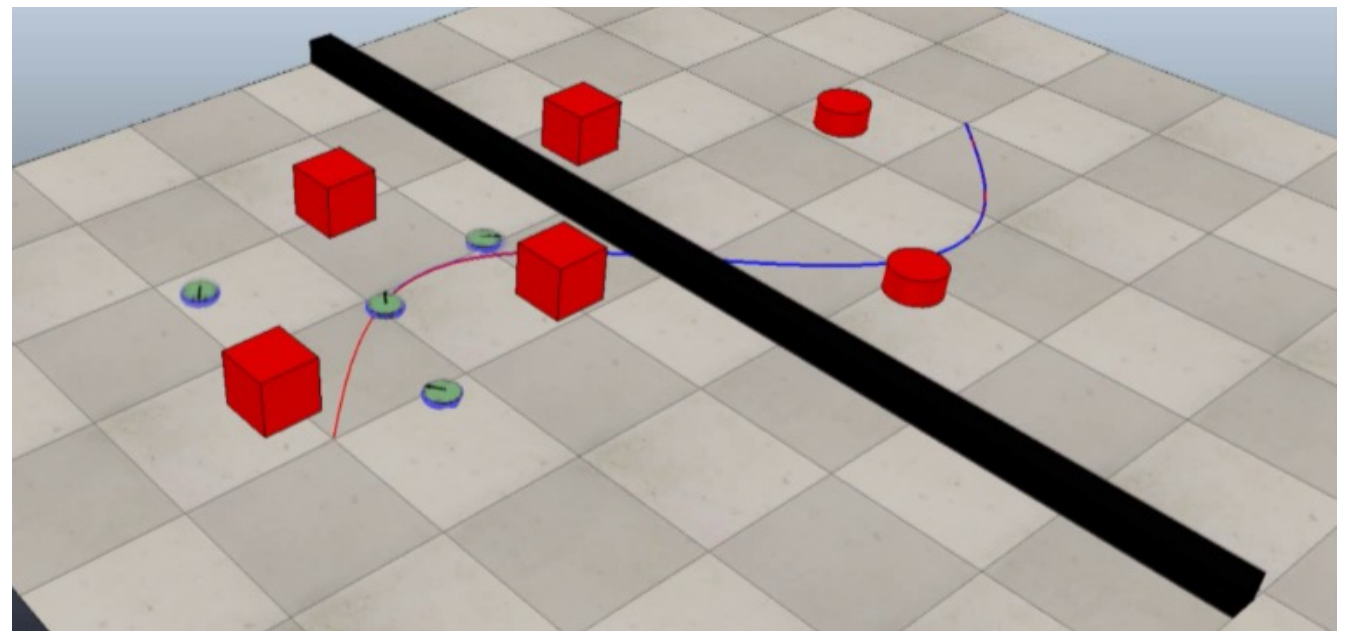
- root the tree at  $(\mathbf{q}_{\text{ini}}, \dot{\mathbf{q}}_{\text{ini}}, 0)$
- iteratively
  - randomly select a **sample**  $\mathbf{y}_{\text{rand}}$
  - compute an **IK solution**  $\mathbf{q}_{\text{rand}} = \mathbf{f}^{-1}(\mathbf{y}_{\text{rand}})$
  - randomly assign to  $\mathbf{q}_{\text{rand}}$  a time instant  $t_{\text{rand}}$  and a velocity  $\dot{\mathbf{q}}_{\text{rand}}$
  - search the **closest vertex**  $(\mathbf{q}_{\text{near}}, \dot{\mathbf{q}}_{\text{near}}, t_{\text{near}})$  to  $(\mathbf{q}_{\text{rand}}, \dot{\mathbf{q}}_{\text{rand}}, t_{\text{rand}})$ , and extract  $s_k$  associated to  $\mathbf{q}_{\text{near}}$
  - generate **accelerating/decelerating motions**
    - **time histories**: randomly choose two values of  $\ddot{s}$  (pos/neg)
    - **subpaths**: numerically integrate using random  $\tilde{\mathbf{z}}$ 
$$\mathbf{q}'' = \mathbf{J}^\# (\mathbf{y}_d'' - \mathbf{J}' \mathbf{q}' + k_p \mathbf{e}_y + k_d \mathbf{e}'_y) + (\mathbf{I} - \mathbf{J}^\# \mathbf{J}) \tilde{\mathbf{z}}$$
  - if **no violation** occurs, add new vertices and edges to the tree

# exploration-exploitation

improve the search efficiency and/or the quality of the solution by altering

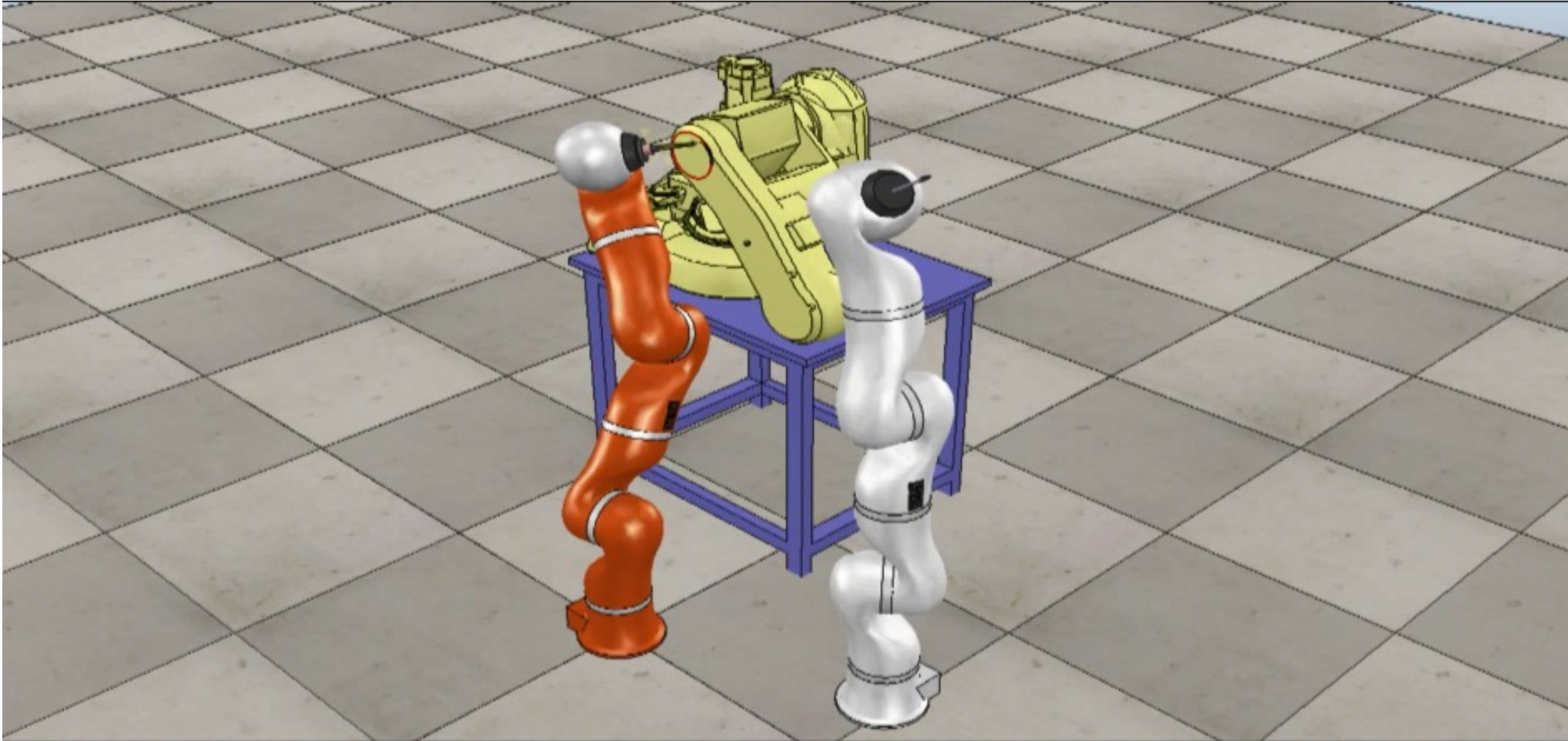
- **exploration**
  - residual input ( $\tilde{W}$  or  $\tilde{Z}$ ) chosen **randomly**
  - essential for guaranteeing **probabilistic completeness**
- **exploitation**
  - residual input ( $\tilde{W}$  or  $\tilde{Z}$ ) chosen **deterministically** with the objective of minimizing a certain state-dependent cost function

example: minimize the centroidal variance of a formation of mobile robots





# V-REP simulations



the orange KUKA LWR manipulator must perform a welding task (red circle) while avoiding another LWR (white) moving in its workspace

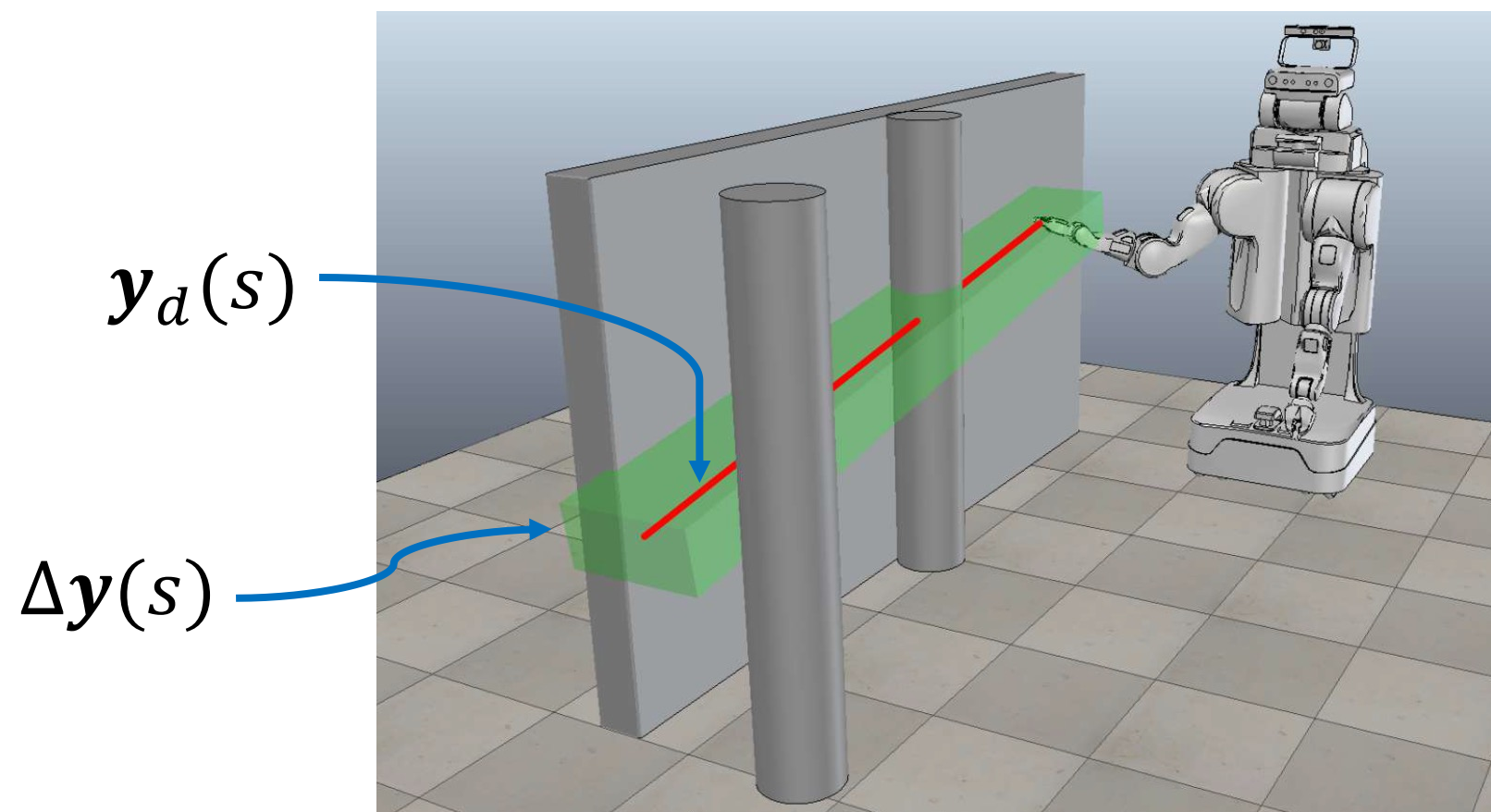


# soft task-constrained motion planning (STCMP)

- **problem**: find **feasible, collision-free** motions for a robot that is assigned a **soft task constraint** in an environment containing obstacles
- the robot **configuration**  $q$  takes values in a  $n_q$ -dimensional configuration space  $\mathcal{C}$ , containing a free part  $\mathcal{C}_{\text{free}}$
- the **task** is described in coordinates  $y$  taking values in a  $n_y$ -dimensional task space  $\mathcal{Y}$
- **assumptions**
  - the robot is **kinematically redundant** w.r.t. the task ( $n_q > n_y$ )
  - obstacles are **fixed**
  - the robot is **free-flying** in  $\mathcal{C}$ , then its kinematic model consists of simple integrators and is expressed in geometric form as  $q' = \tilde{v}$

# soft task constraints

- the **soft task constraint** is defined by
  - a **desired task path**  $\mathbf{y}_d(s)$ ,  $s \in [0,1]$
  - a **tolerance**  $\Delta\mathbf{y}(s)$ ,  $s \in [0,1]$ , a positive  $n_y$ -vector that represents for each component the max admissible deviation of  $\mathbf{y}$  from  $\mathbf{y}_d$  at  $s$



- the tolerance can be exploited whenever realizing the desired task exactly is **difficult** or **impossible** (**narrow** or **closed** passages in  $\mathcal{C}$ )

# STCMP

- the **task error** associated to  $\mathbf{q}$  at  $s$  is  $\mathbf{e}(\mathbf{q}, s) = \mathbf{y}_d(s) - \mathbf{f}(\mathbf{q}(s))$
- $\mathbf{q}$  is **compliant** with the **hard task** at  $s$  if  $\mathbf{e}(\mathbf{q}, s) = 0$

$$\mathcal{L}(s) = \{\mathbf{q} \in \mathcal{C} : \mathbf{e}(\mathbf{q}, s) = 0\} \quad \longrightarrow \quad \mathcal{C}_{\text{hard}} = \bigcup_{s \in [0,1]} \mathcal{L}(s)$$

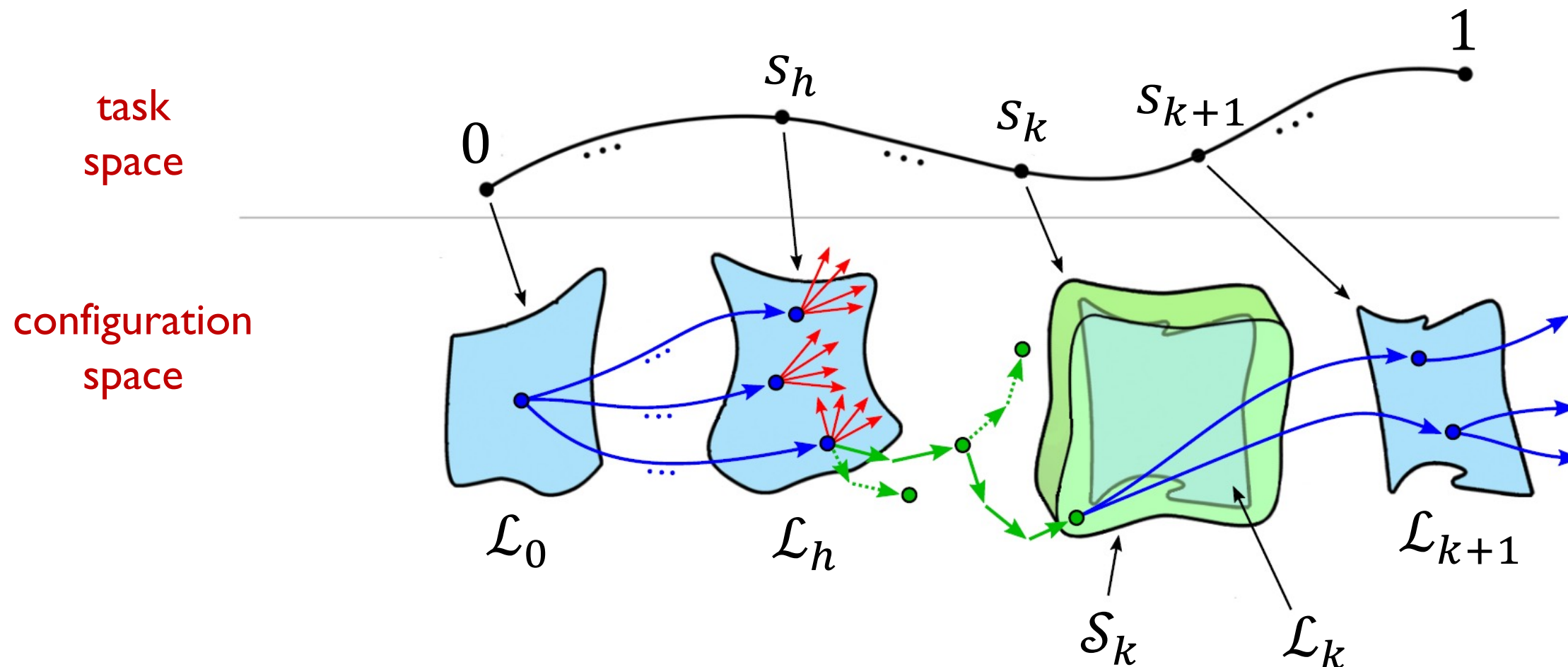
- $\mathbf{q}$  is **compliant** with the **soft task** at  $s$  if  $|\mathbf{e}(\mathbf{q}, s)| \leq \Delta \mathbf{y}(s)$

$$\mathcal{S}(s) = \{\mathbf{q} \in \mathcal{C} : \mathbf{e}(\mathbf{q}, s) \leq \Delta \mathbf{y}(s)\} \quad \longrightarrow \quad \mathcal{C}_{\text{soft}} = \bigcup_{s \in [0,1]} \mathcal{S}(s)$$

- **solution**: a **configuration-space path**  $\mathbf{q}(s)$ ,  $s \in [0,1]$ , such that for all  $s$ :
  - $\mathbf{q}(s)$  is compliant with the soft task
  - (self-)collisions, singularities and joint limits violations are avoided
- but: **the solution should comply with the hard task as much as possible**

# opportunistic planner

- builds a **tree**  $\mathcal{T}$  in  $\mathcal{C}_{\text{soft}} \cap \mathcal{C}_{\text{free}}$  alternating two (sub)planners
  - the **hard planner (HP)** extends  $\mathcal{T}$  as much as possible in  $\mathcal{C}_{\text{hard}}$
  - when HP identifies an obstruction, the **soft planner (SP)** extends  $\mathcal{T}$  in  $\mathcal{C}_{\text{soft}}$  until extension by HP is viable again



- **frontier index  $h$** : index of the largest sample of  $s$  for which there exists a vertex  $q$  in  $\mathcal{T}$  on  $\mathcal{L}_h$  or  $\mathcal{S}_h$

# hard planner

generic iteration

1. generate a **random configuration**  $\mathbf{q}_{\text{rand}}$  in  $\mathcal{C}_{\text{hard}}$
2. select in  $\mathcal{T}$  the **closest vertex**  $\mathbf{q}_{\text{near}}$  to  $\mathbf{q}_{\text{rand}}$
3. produce a **subpath** from  $\mathbf{q}_{\text{near}} \in \mathcal{L}_j$  to  $\mathbf{q}_{\text{new}} \in \mathcal{L}_{j+1}$  by integrating

$$\tilde{\mathbf{v}} = \mathbf{J}^\#(\mathbf{q})(\mathbf{y}'_d + \mathbf{K}\mathbf{e}(\mathbf{q})) + (\mathbf{I} - \mathbf{J}^\#(\mathbf{q})\mathbf{J}(\mathbf{q}))\tilde{\boldsymbol{\omega}}$$

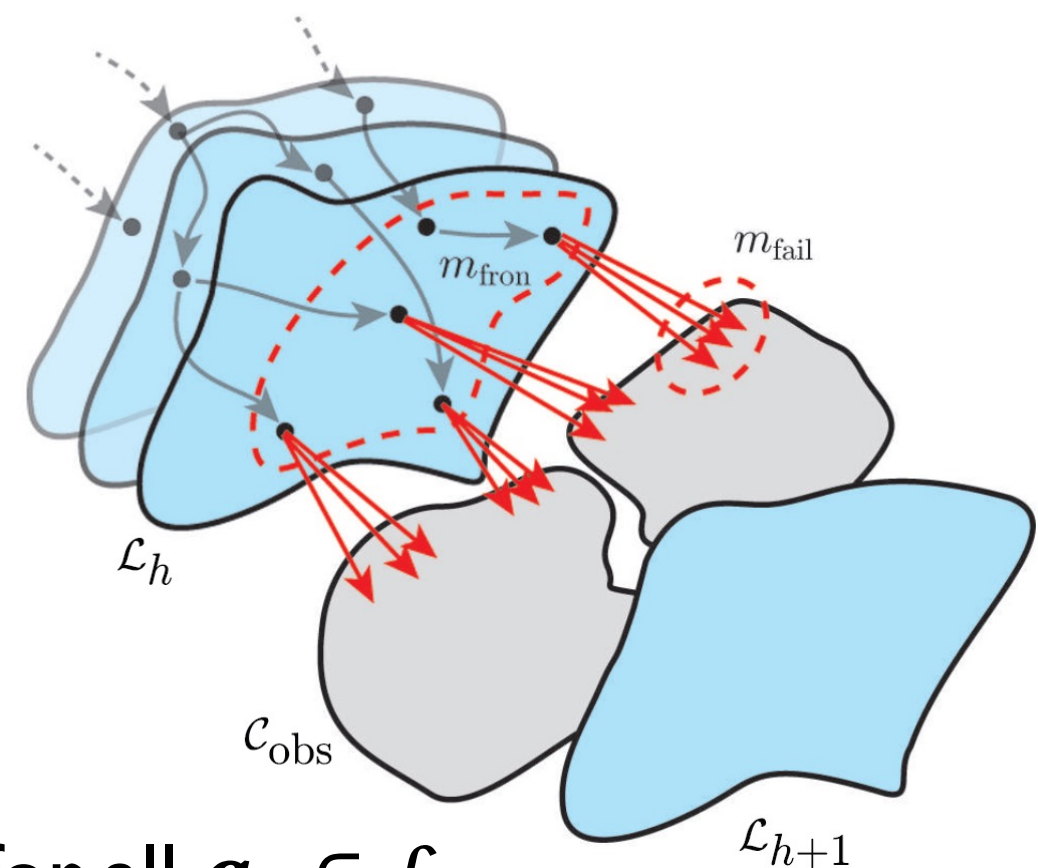
4. **if** the subpath is **valid**

- **extend**  $\mathcal{T}$
- if  $\mathbf{q}_{\text{new}} \in \mathcal{L}_{h+1}$ , **update**  $h$

**else**

- increase **failure counter**  $m_{\text{fail}}(\mathbf{q}_{\text{near}})$
- detect presence of **obstruction** if

$$m_{\text{fron}} \geq m_{\text{fron}}^{\text{max}} \text{ and } m_{\text{fail}}(\mathbf{q}_j) \geq m_{\text{fail}}^{\text{max}} \text{ for all } \mathbf{q}_j \in \mathcal{L}_h$$

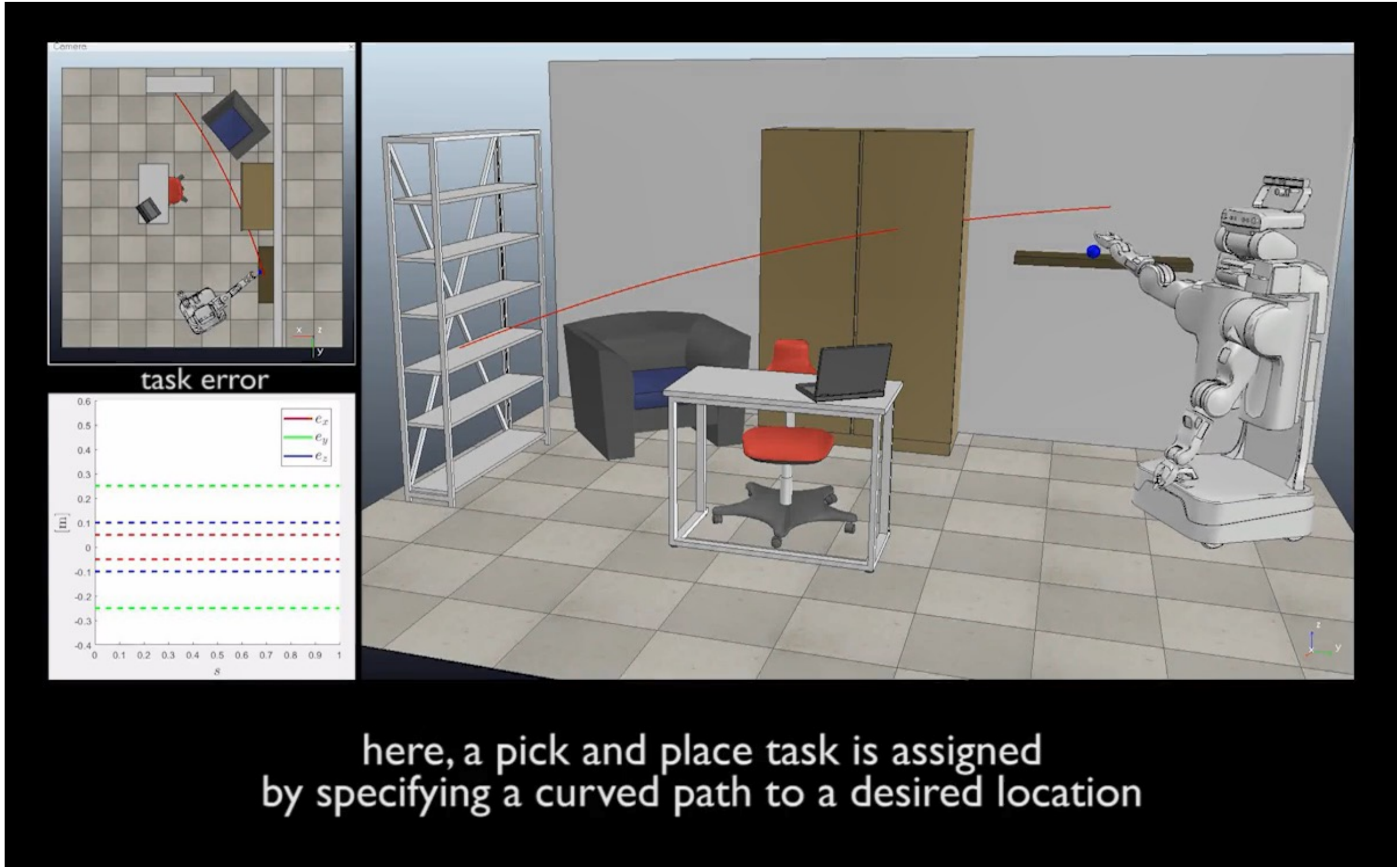


# soft planner

- identify  $s_k$  where the **obstruction disappears** as the first sample beyond  $s_h$  where  $m_{\text{free}} \geq m_{\text{free}}^{\min}$  collision-free IK solutions exist
- grow a tree  $\mathcal{T}_{\text{soft}}$  in  $\mathcal{C}_{\text{soft}}$  to find a **subpath connecting  $\mathcal{L}_h$  to  $\mathcal{S}_k$**
- root  $\mathcal{T}_{\text{soft}}$  at a random vertex  $q_h$  of  $\mathcal{T}$  lying on  $\mathcal{L}_h$
- generic iteration
  1. generate a **random configuration**  $q_{\text{rand}}$  in  $\mathcal{C}_{\text{free}}$
  2. select in  $\mathcal{T}_{\text{soft}}$  the **closest vertex**  $q_{\text{near}}$  to  $q_{\text{rand}}$
  3. generate  $q_{\text{curr}}$  moving of  $\eta$  from  $q_{\text{near}}$  towards  $q_{\text{rand}}$
  4. iteratively compute
$$q_{\text{curr}} = q_{\text{curr}} - \eta \frac{J^T(q_{\text{curr}})e(q_{\text{curr}}, s_{\text{curr}} + \delta s)}{\|J^T(q_{\text{curr}})e(q_{\text{curr}}, s_{\text{curr}} + \delta s)\|}$$
until  **$\mathcal{S}_k$  is reached** or  **$q_{\text{curr}}$  not valid/compliant** with the soft task
  5. **extend**  $\mathcal{T}_{\text{soft}}$



# V-REP simulations



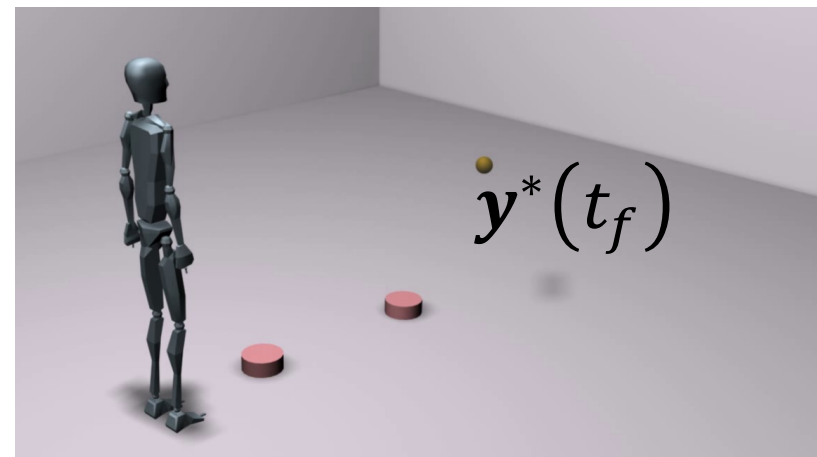
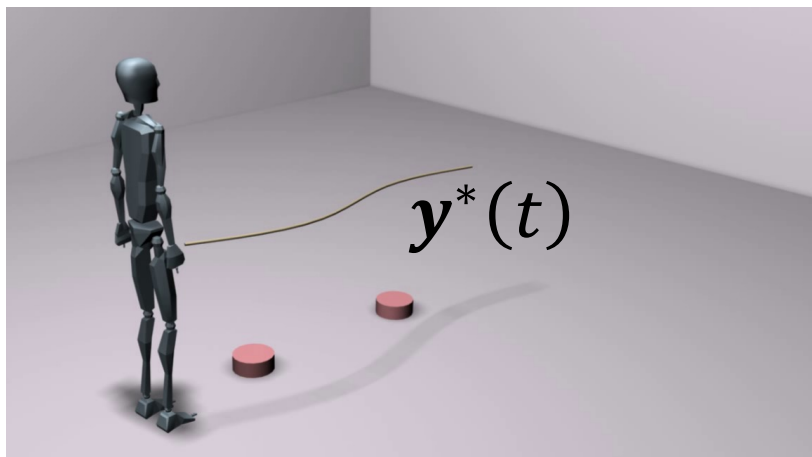


# whole-body motion planning for humanoid robots

- **problem**: find **feasible, collision-free** whole-body motions for a humanoid that is assigned a task whose execution may require **walking**
- the generic **humanoid configuration** is

$$\mathbf{q} = \begin{pmatrix} \mathbf{q}_{\text{CoM}} \\ \mathbf{q}_{\text{jnt}} \end{pmatrix} \quad \begin{array}{l} \text{pose of the CoM frame} \\ n\text{-vector of joint angles} \end{array}$$

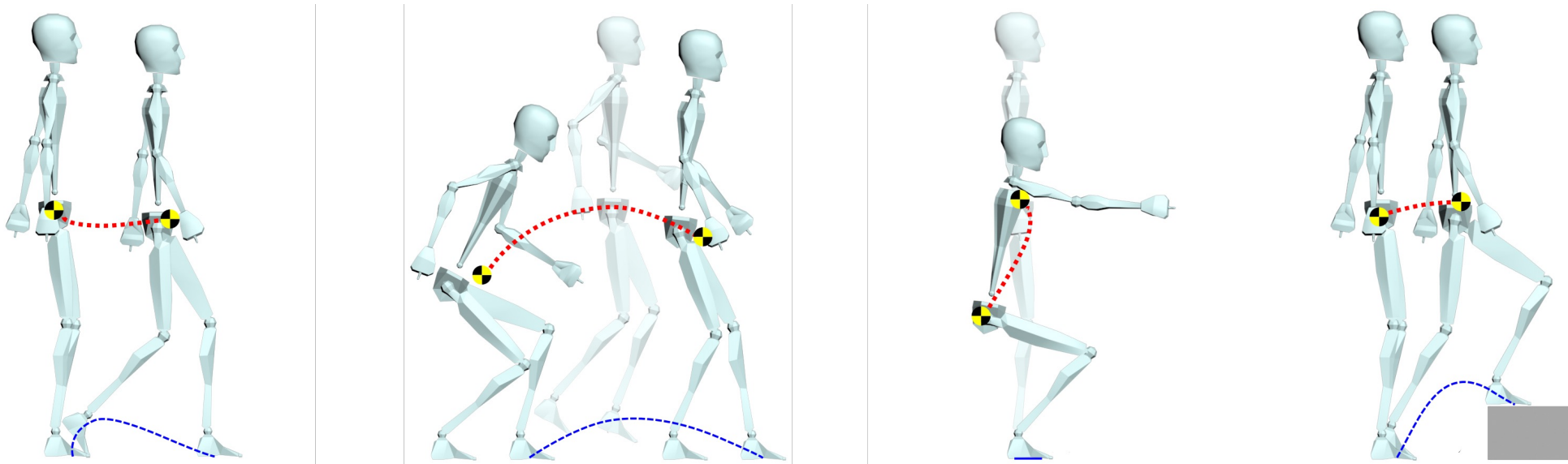
- the **task** is defined by a **desired trajectory**  $\mathbf{y}^*(t)$  (or a geometric path  $\mathbf{y}^*(s)$  or a single point  $\mathbf{y}^*(t_f)$ ) for a specific point of the humanoid



- **solution** to the planning problem: a whole-body motion, i.e., a **configuration-space trajectory**  $q(t)$ , such that
  - the **assigned task** is realized
  - **collisions** with workspace obstacles and **self-collisions** are avoided
  - position and velocity **limits** on the robot joints are satisfied
  - the robot is in **equilibrium** at all times
- most approaches rely on a **separation** between locomotion and task execution, thus failing to exploit the rich humanoid motion capabilities
- our approach
  - **does not separate** locomotion from task execution, taking advantage of the whole-body structure of the humanoid
  - walking **emerges naturally** from the solution

# planning based on CoM movement primitives

- **main idea**: build a solution by concatenating various feasible whole-body motions that realize **CoM movement primitives** contained in a precomputed catalogue



- a CoM movement primitive  $\mathbf{u}_{\text{CoM}}$ 
  - represents an **elementary humanoid motion** (e.g., walking, jumping)
  - is characterized by a **duration**  $T$ , a **CoM reference trajectory**  $\mathbf{z}_{\text{CoM}}^*(t)$  and a **swing foot reference trajectory**  $\mathbf{z}_{\text{swg}}^*(t)$
  - **does not** specify a whole-body joint motion

# motion generation

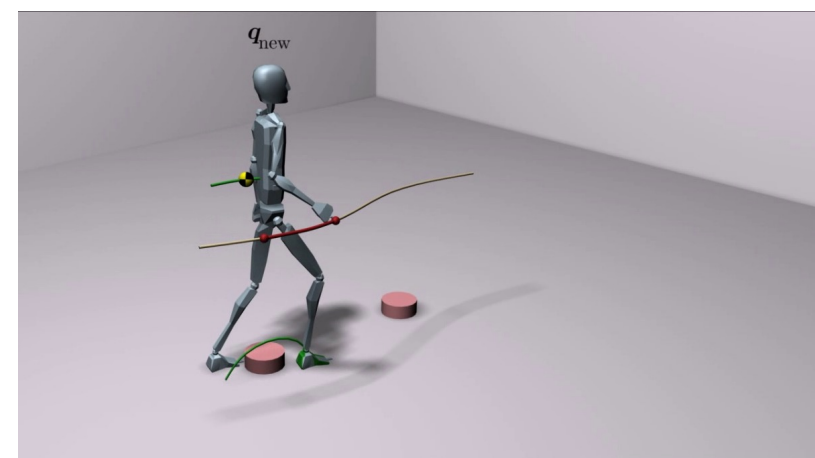
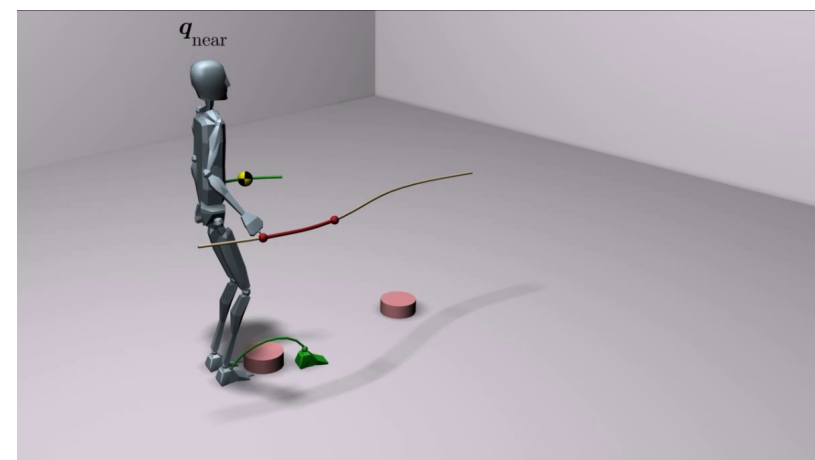
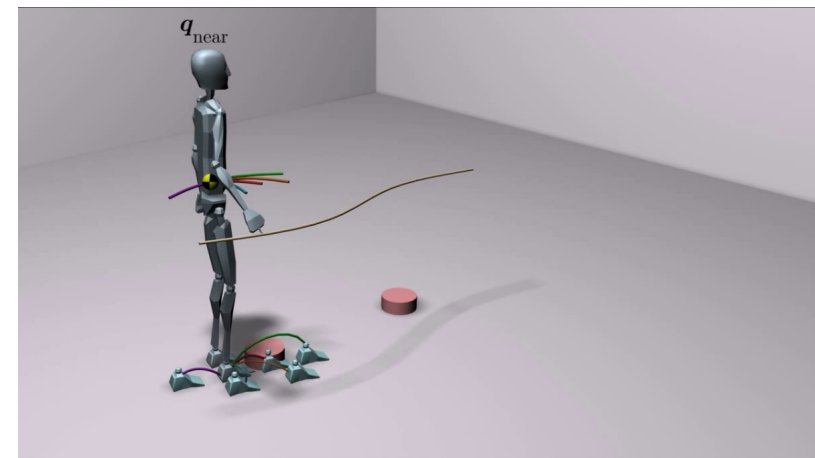
- the planner works iteratively, by repeated calls to a **motion generator**
- it is invoked from a certain configuration  $\mathbf{q}_k$  at time  $t_k$

1. **CoM primitive selection**: select a CoM primitive by randomly picking from the **catalogue**

$$U = \{U_{\text{CoM}}^S \cup U_{\text{CoM}}^D \cup \text{free\_CoM}\}$$

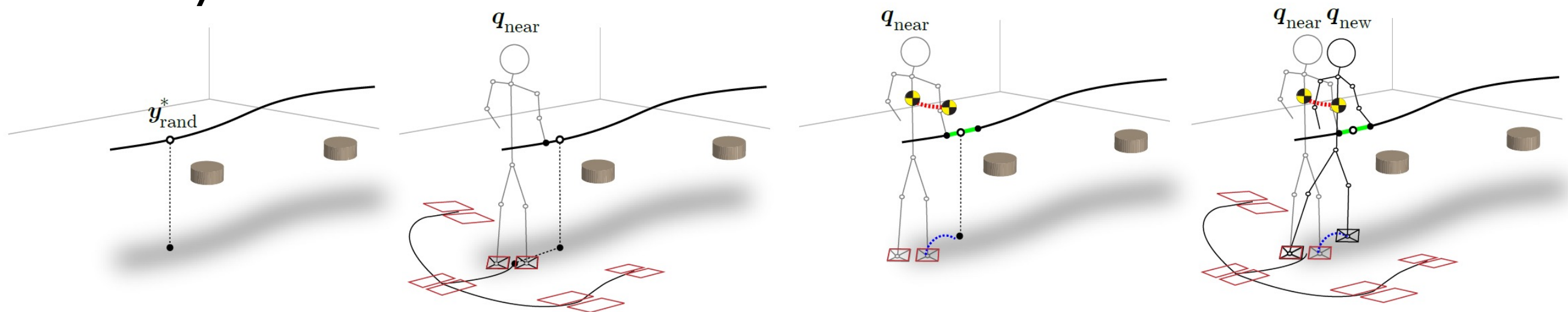
2. **joint motion generation**: produce joint motion from  $\mathbf{q}_k$  at  $t_k$  that realizes the **selected CoM primitive** and the **portion of the assigned task** in  $[t_k, t_{k+1}]$  by integrating

$$\dot{\mathbf{q}}_{\text{jnt}} = \mathbf{J}_a^\# (\dot{\mathbf{y}}_a^* + \mathbf{K}\mathbf{e}) + (\mathbf{I} - \mathbf{J}_a^\# \mathbf{J}_a) \boldsymbol{\omega}$$



# planner overview

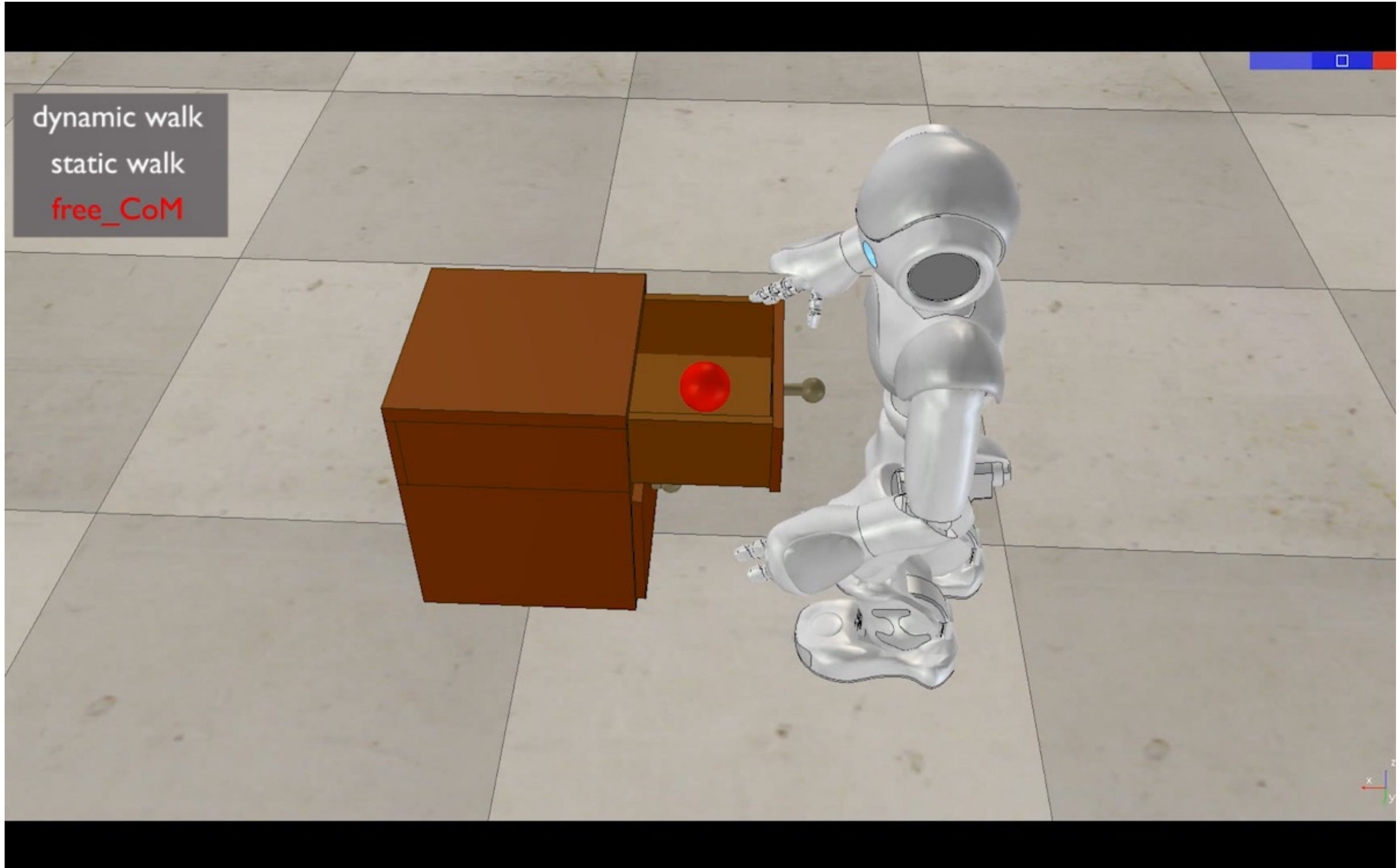
iteratively build a **tree**



1. choose a **random sample**  $y_{\text{rand}}^*$  on the assigned task trajectory
2. extract a configuration  $q_{\text{near}}$  with probability proportional to a **task compatibility function**  $\gamma(\cdot, y_{\text{rand}}^*)$
3. select a random **CoM primitive** and extract the **portion** of the task trajectory to be executed
4. generate the **joint motion** to realize the CoM primitive and the portion of the task
5. if the motion is feasible and collision-free, **add** the final configuration  $q_{\text{new}}$  to the tree

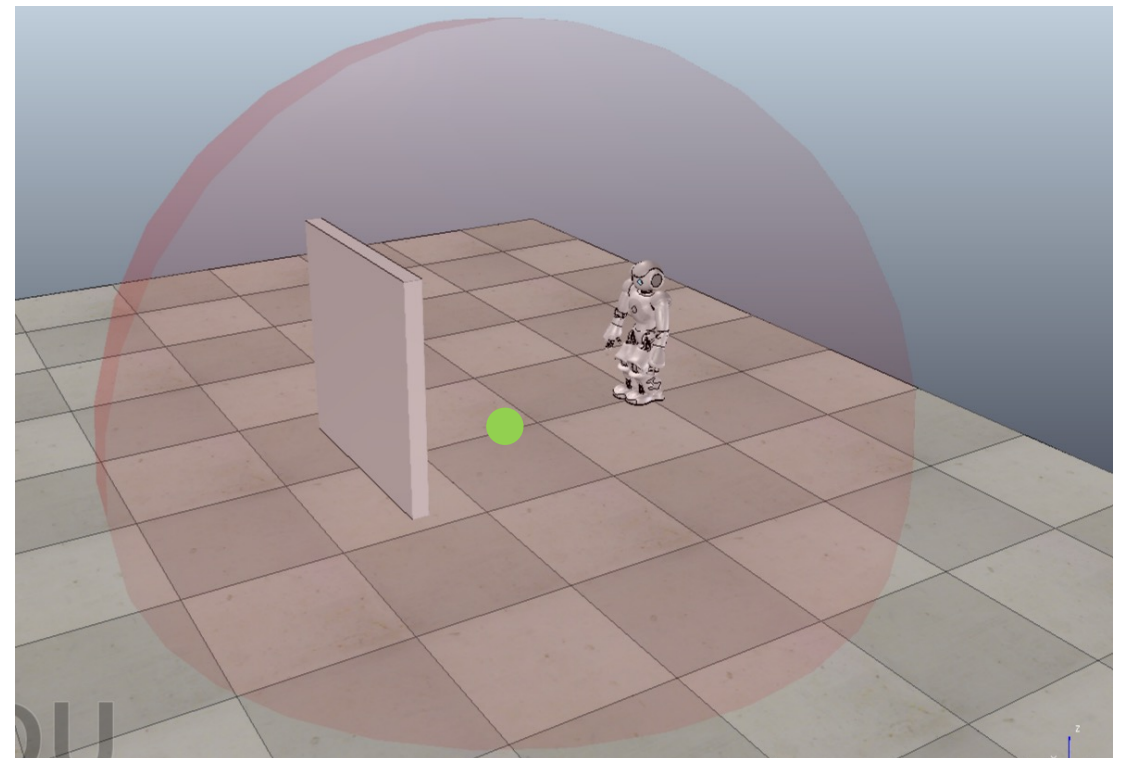
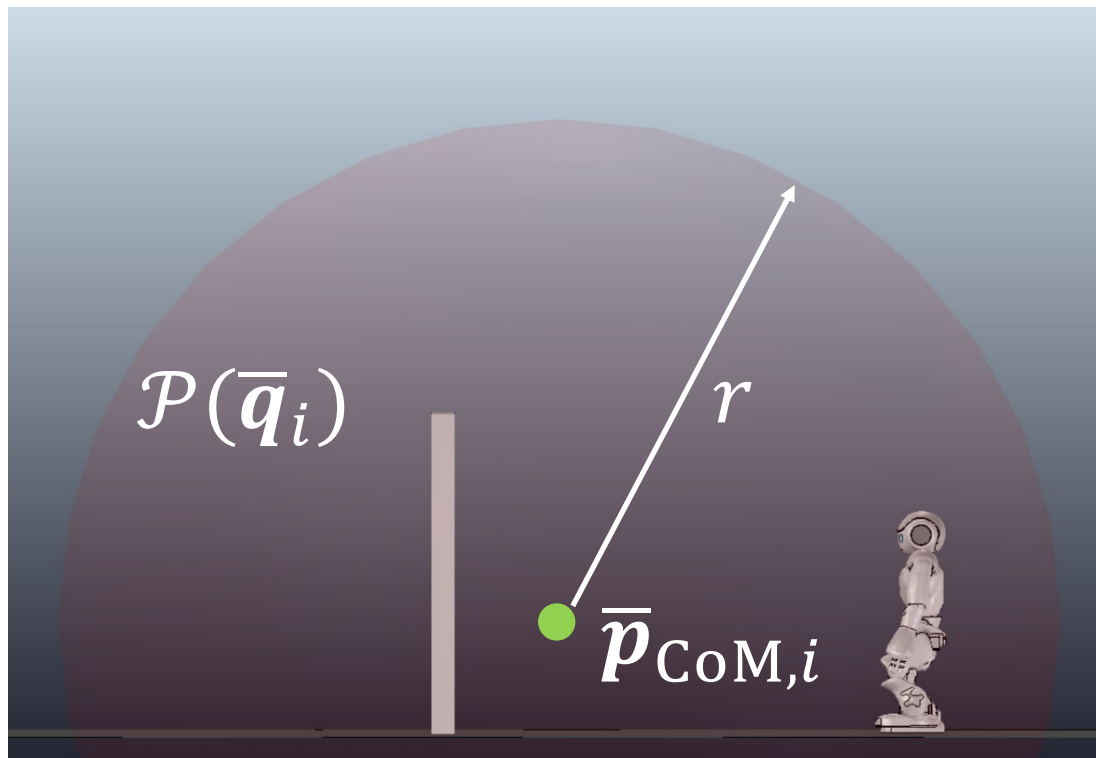


# V-REP simulations



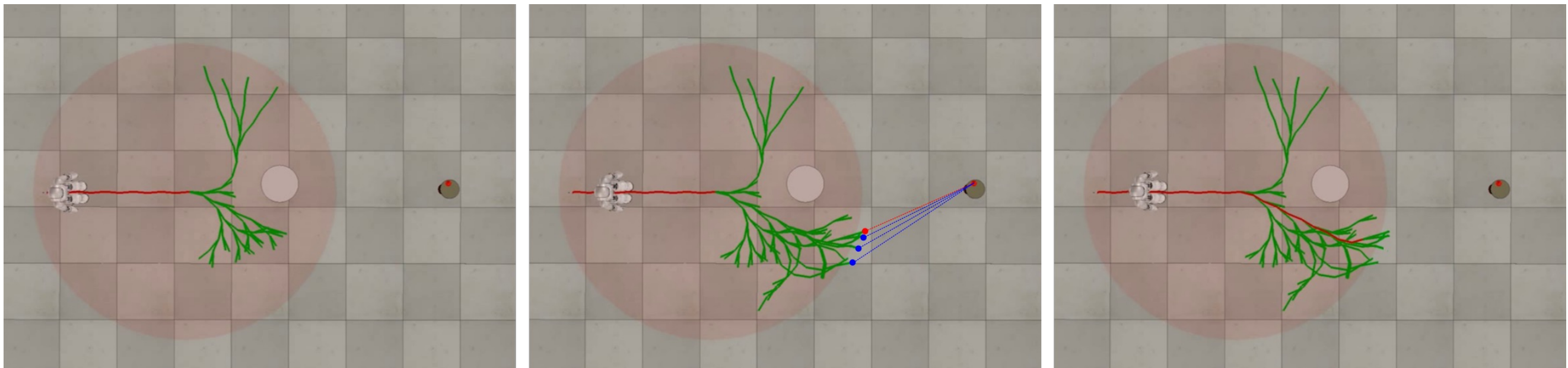
# anytime whole-body planning

- **problem**: plan the humanoid motion under **time limitations**
- **approach**: simultaneously perform **planning** and **execution** of local plans:
  - execute the **current** local plan  $\mathbf{q}_{i-1}(t)$ ,  $t \in [t_{i-1}, t_i]$
  - plan the **next** local plan  $\mathbf{q}_i(t)$ ,  $t \in [t_i, t_{i+1}]$ , that
    - starts at  $\bar{\mathbf{q}}_i = \mathbf{q}_{i-1}(t_i)$
    - is feasible within a limited **planning zone**  $\mathcal{P}(\bar{\mathbf{q}}_i)$



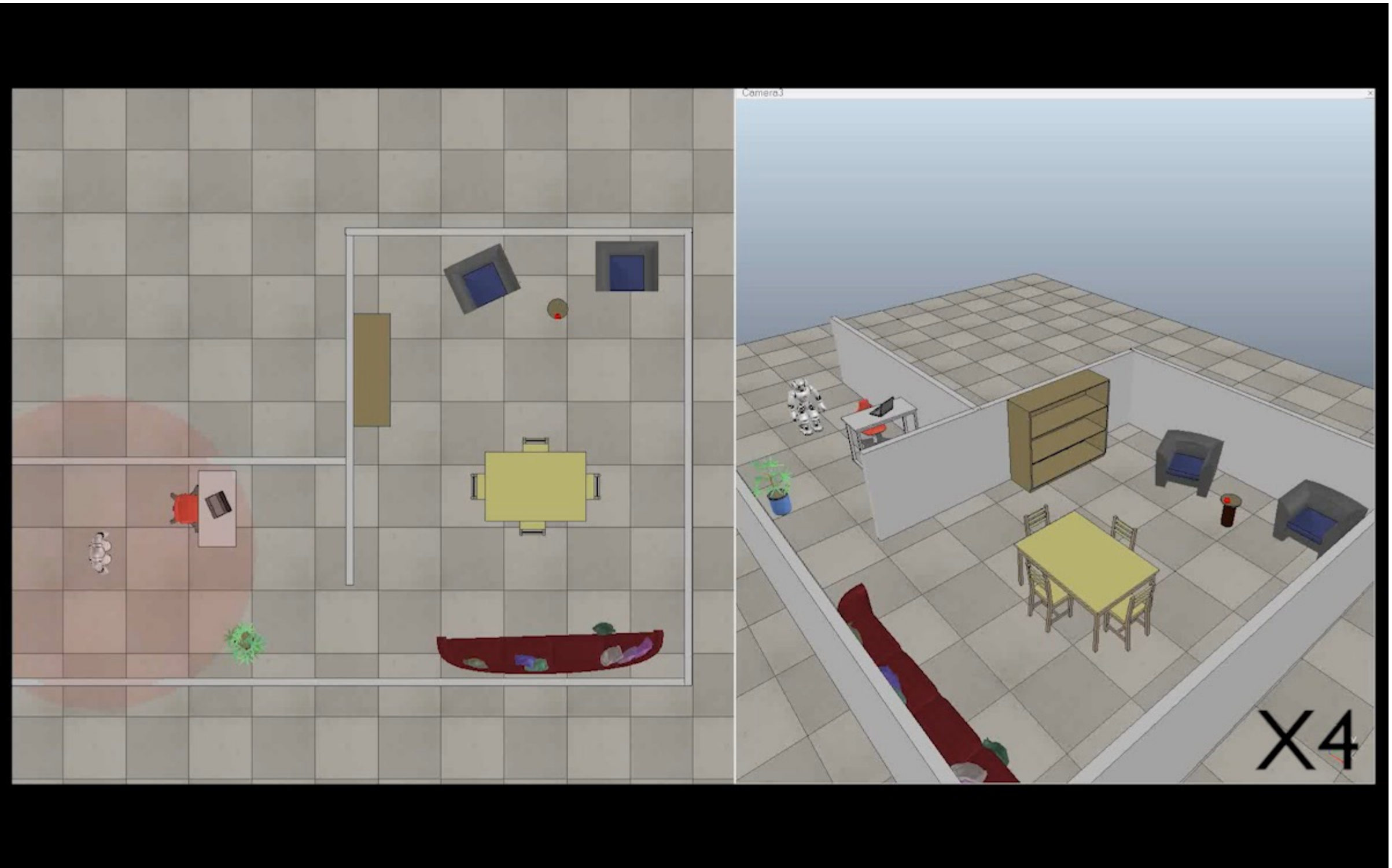
# local motion planner

- runs for a given time budget  $\Delta T_P$
- works in **two stages**
  - **lazy stage**: quickly populate  $\mathcal{T}$  with partial configurations  $\mathbf{q} = (\mathbf{q}_{\text{CoM}}, \emptyset)$ , checking collisions **only** at vertexes using a **simplified occupancy volume** for the robot
  - **validation stage**: generate the joint motion  $\mathbf{q}_{\text{jnt}}(t)$  associated to the best candidate plan, checking collisions **both** at vertexes and along edges using the **actual occupancy volume** for the robot



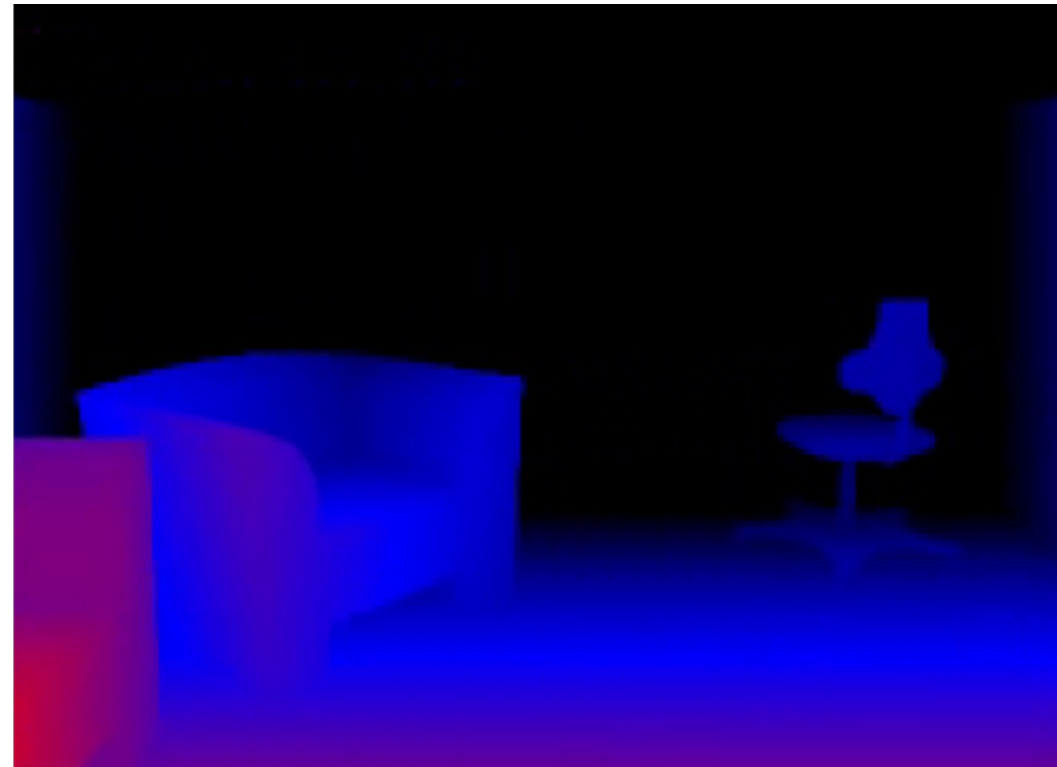
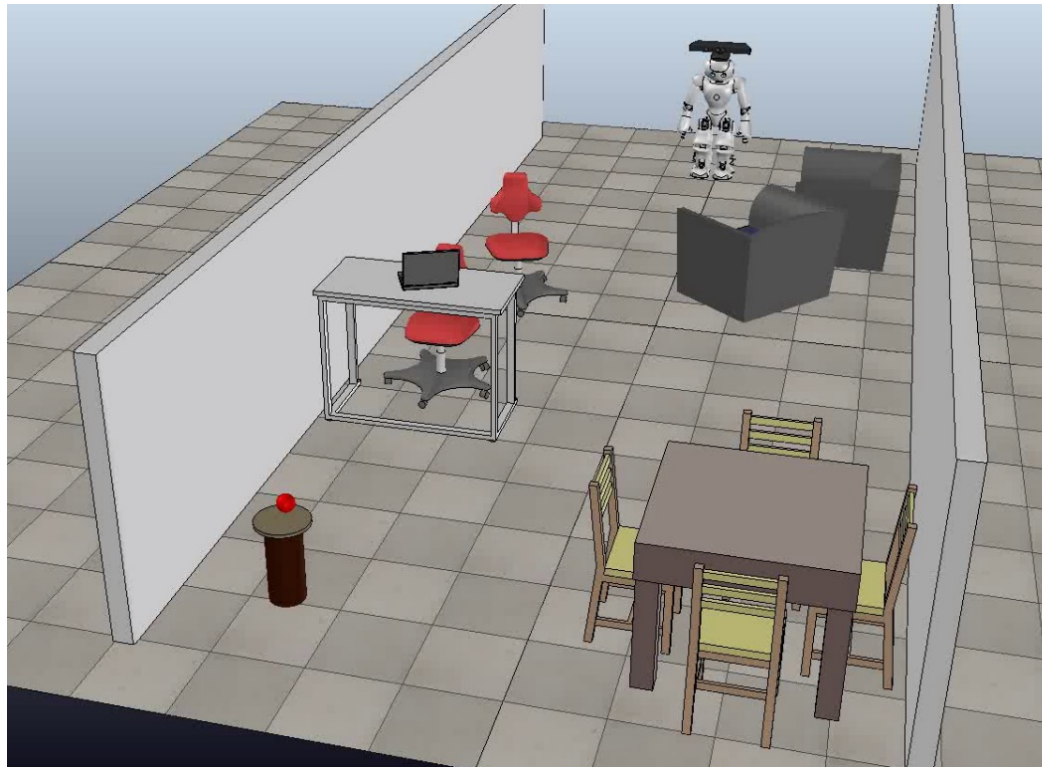


# V-REP simulations



# sensor-based whole-body planning

- **problem:** plan the humanoid motion in **unknown environments**
- the robot is equipped with a head-mounted **depth camera**, e.g., a Kinect
- it is assumed that the robot is localized via an external module



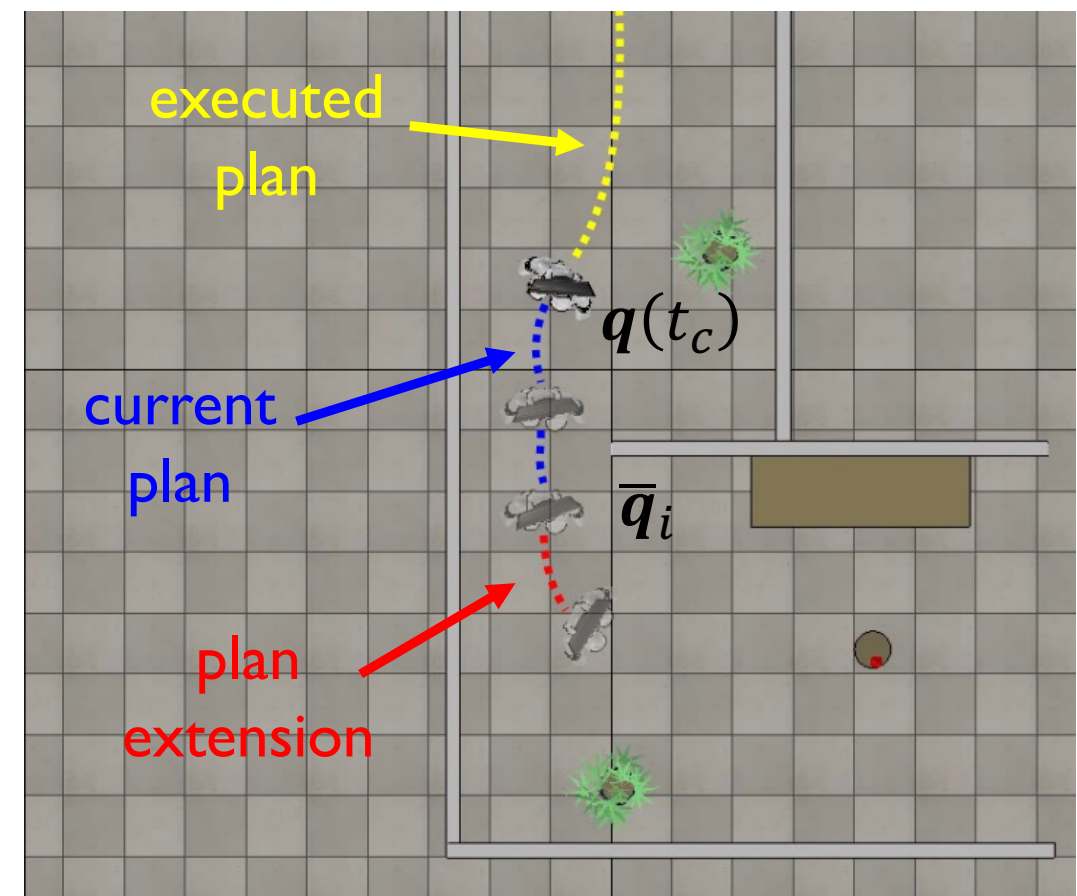
- **approach:** simultaneously perform **mapping**, **planning** and **execution**



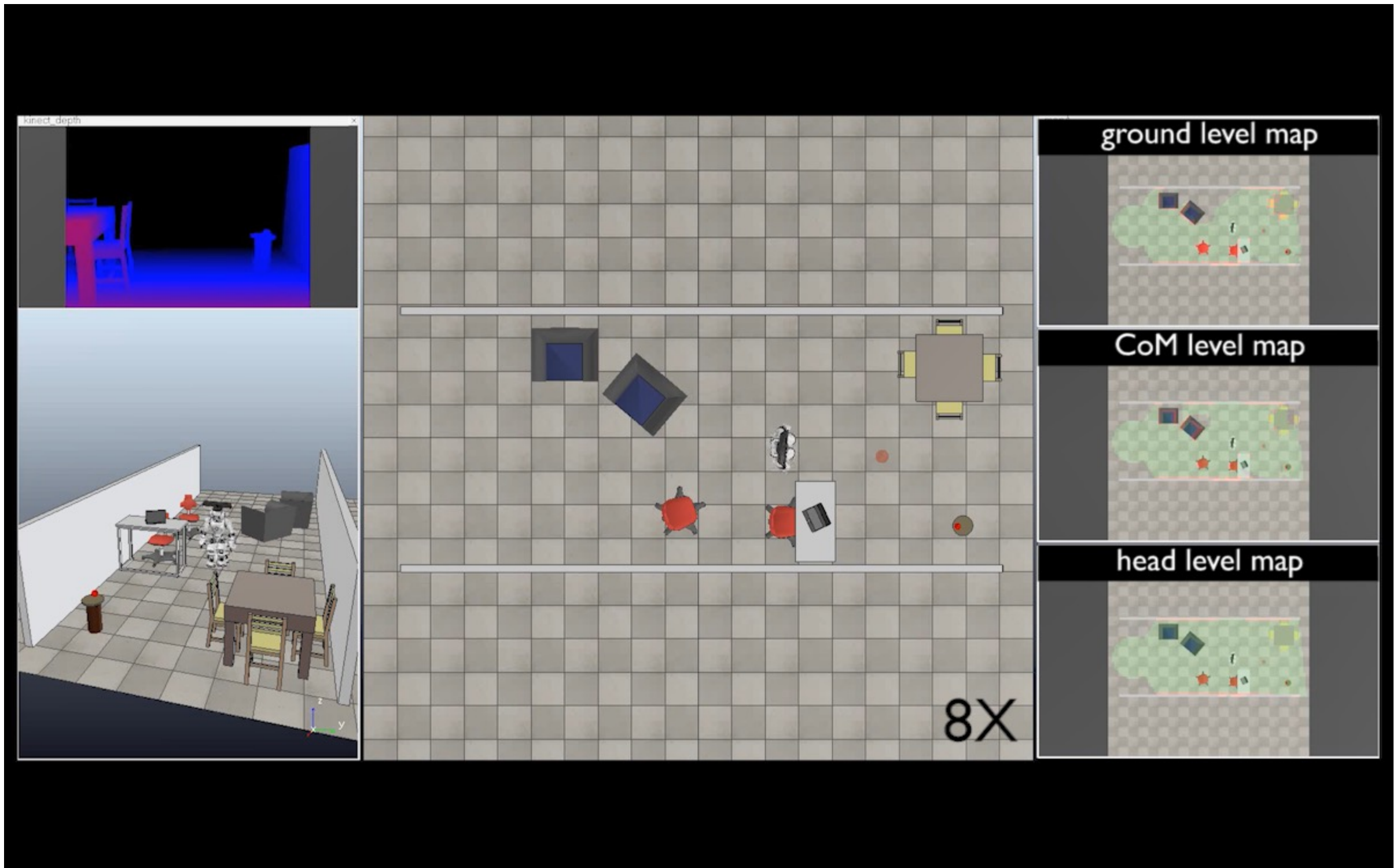
# framework overview

- **mapping module**: continuously **integrates information** gathered by the depth camera into a **3D occupancy grid map**  $\mathcal{M}$
- **execution module**: sends the **commands** to the humanoid actuators based on the **current** plan
- **planning module**: **extends** the current plan with feasible whole-body motions by repeatedly invoking the **local motion planner** providing

- the **final configuration**  $\bar{q}_i$
- the **planning map**  $\mathcal{M}_{P,i} = \mathcal{M}(t_c)$
- the **time budget**  $\Delta T_{P,i} = \alpha_P(t_i - t_c)$

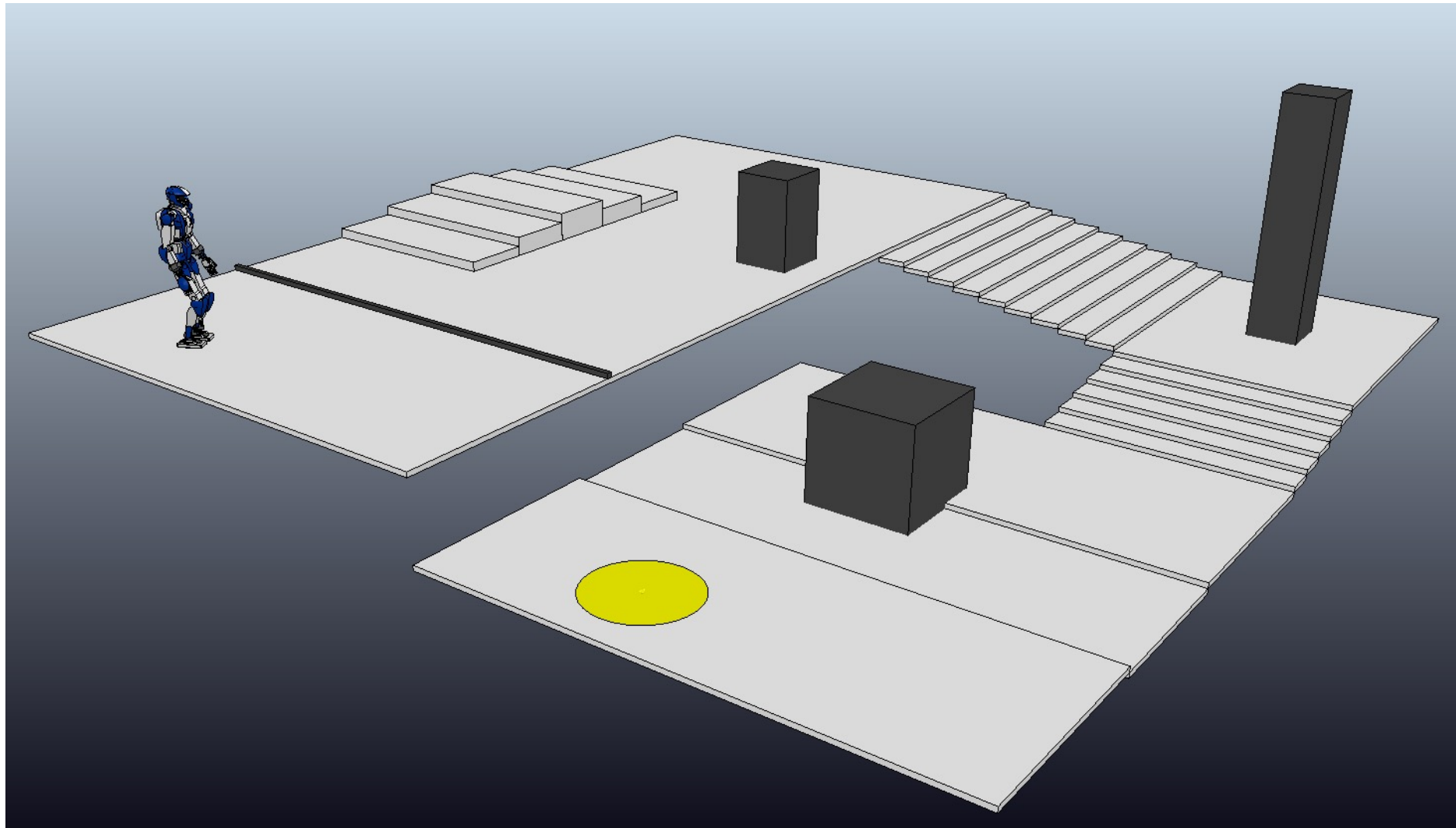


# V-REP simulations



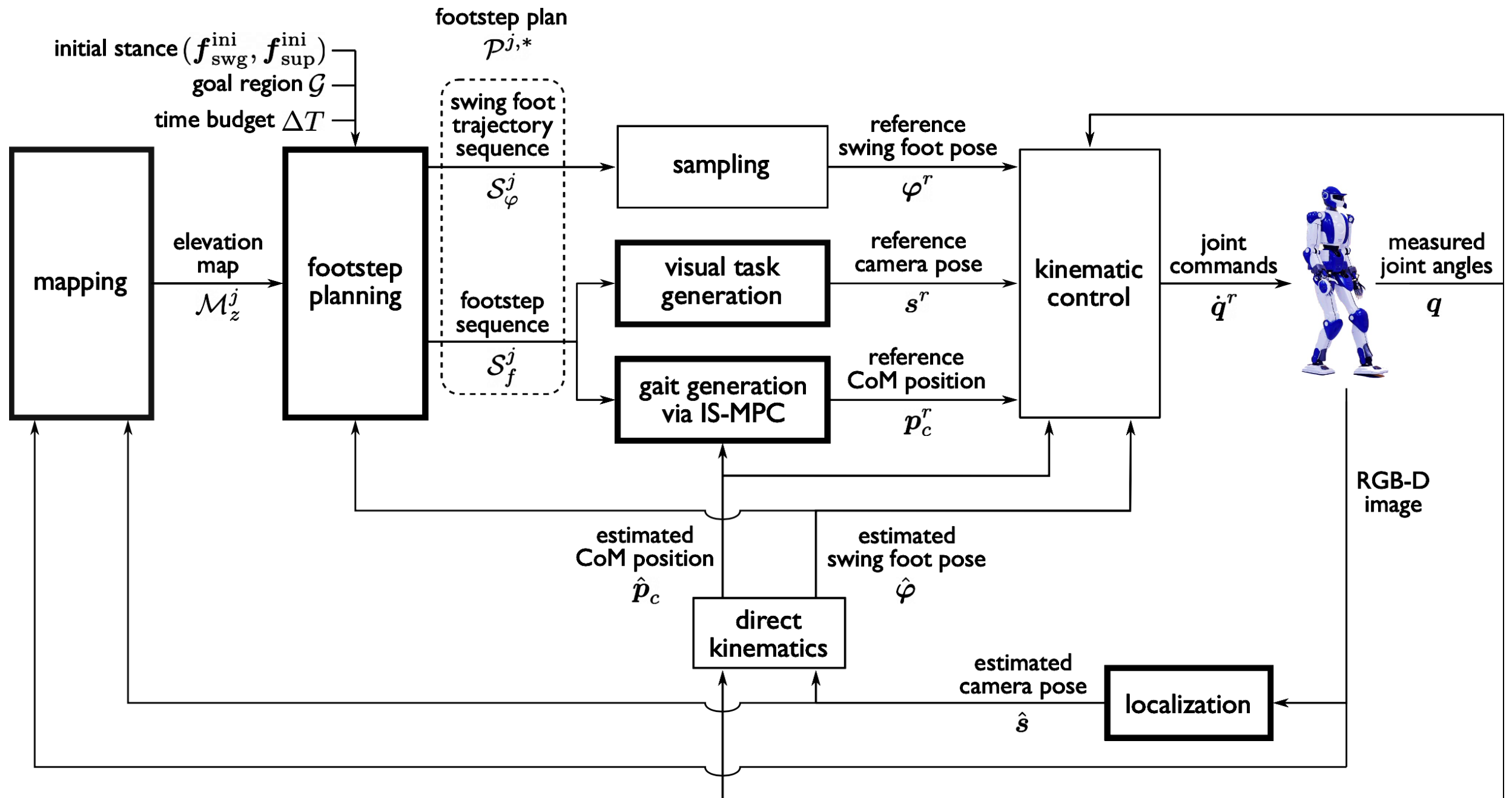
# humanoid motion generation in a world of stairs

- **problem:** generate humanoid motion in an **unknown world of stairs**
- the robot is equipped with a head-mounted **depth camera**
- it is assumed that the robot is localized via an external module



- **approach:** simultaneously perform **mapping**, **planning** and **execution**

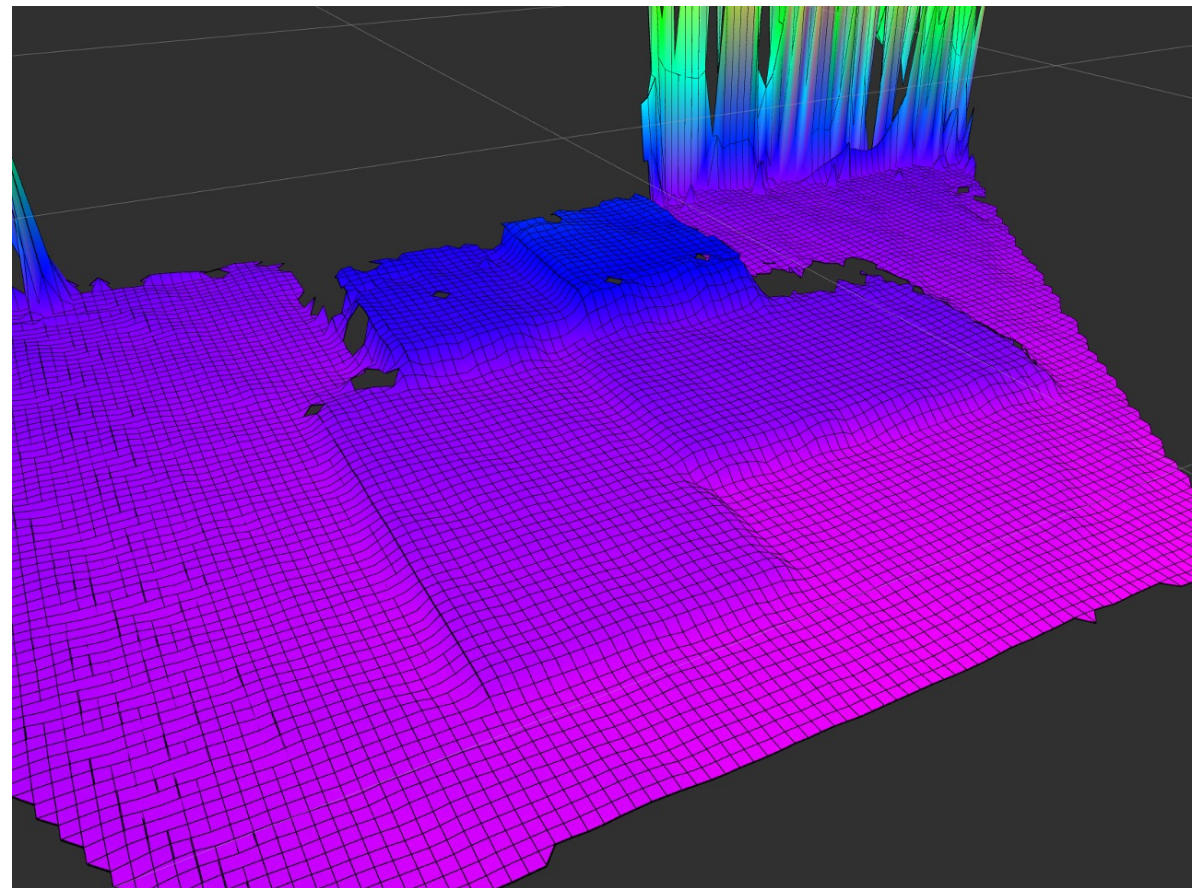
# general architecture





# elevation mapping

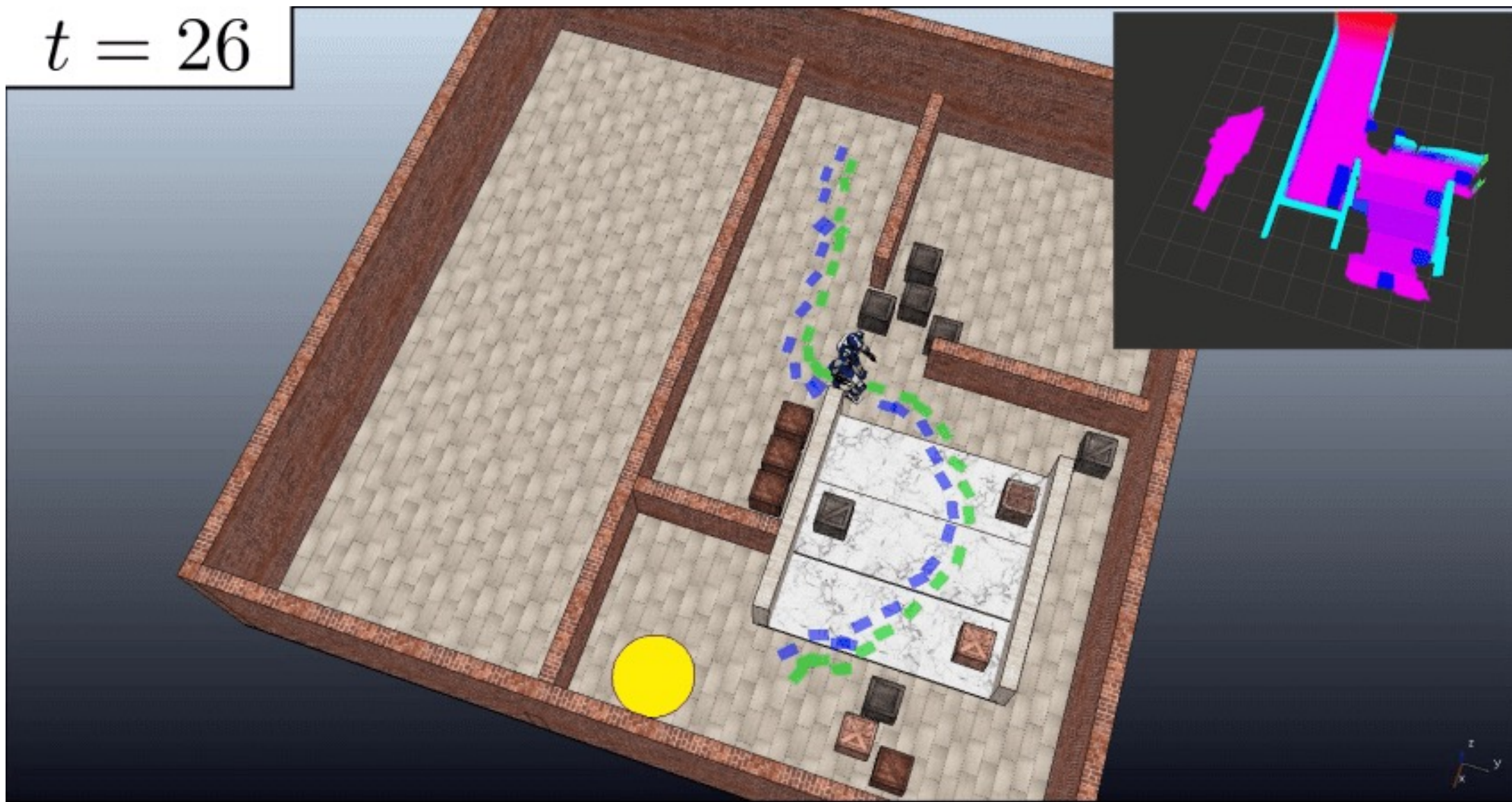
- represent the world of stairs as an **elevation map**
- continuously update the map using on-board sensors
- dynamic environments using visibility check based on ray tracing





# sensor-based footstep planning

- given current stance and current elevation map, generate a **footstep plan** in the direction of an unknown area of the environment
- take advantage of the motion duration to refine the footstep plan



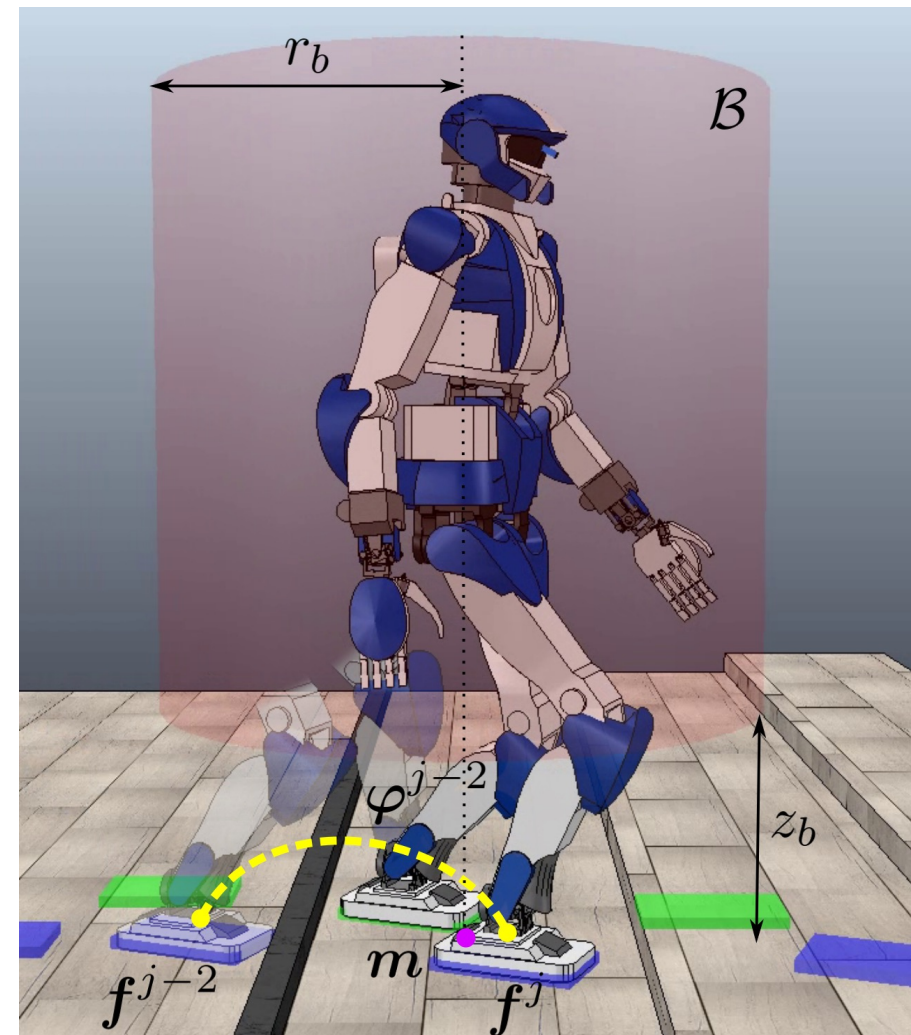
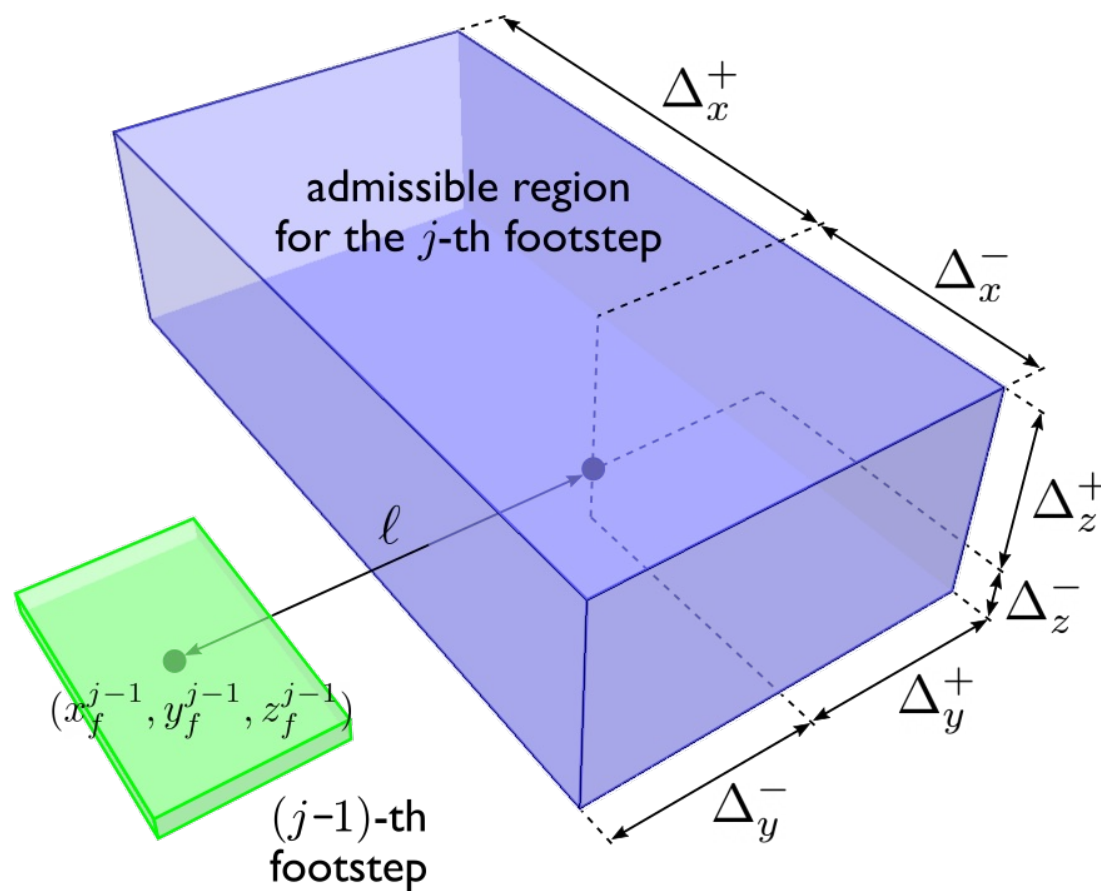
# sensor-based footstep planning: feasibility

- requirements:

R1: footstep fully in contact with a single horizontal patch

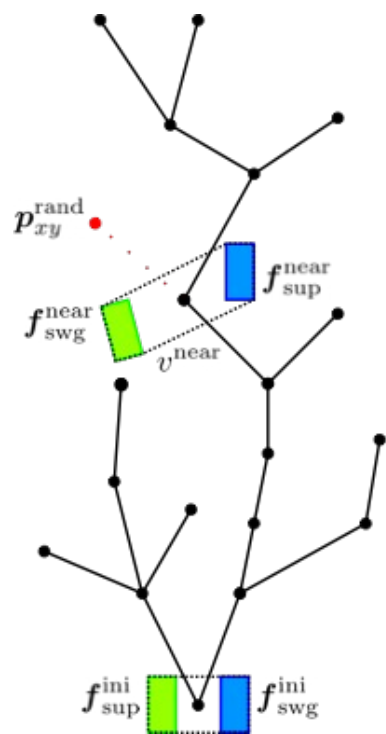
R2: stance feasibility

R3: step feasibility

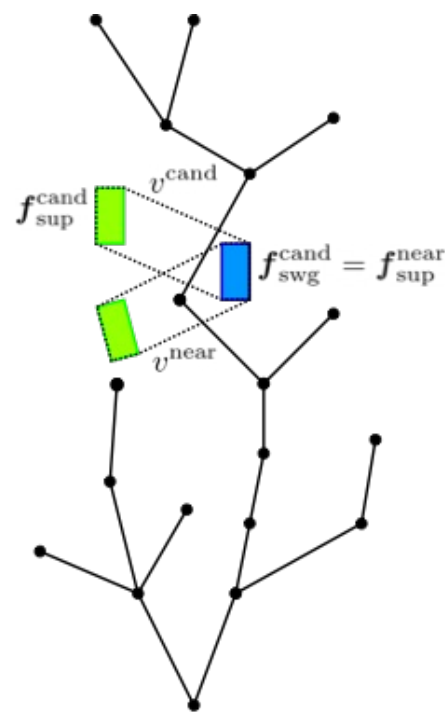


# sensor-based footstep planning: algorithm

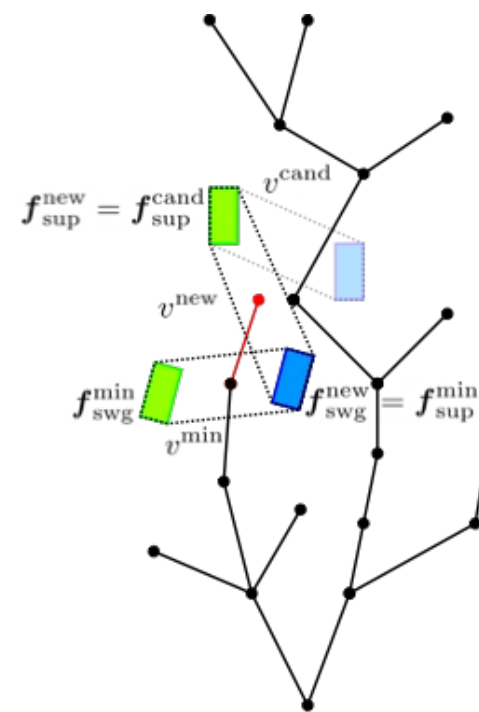
- **RRT\*-based footstep planner** optimizing for number of steps, height variation or clearance



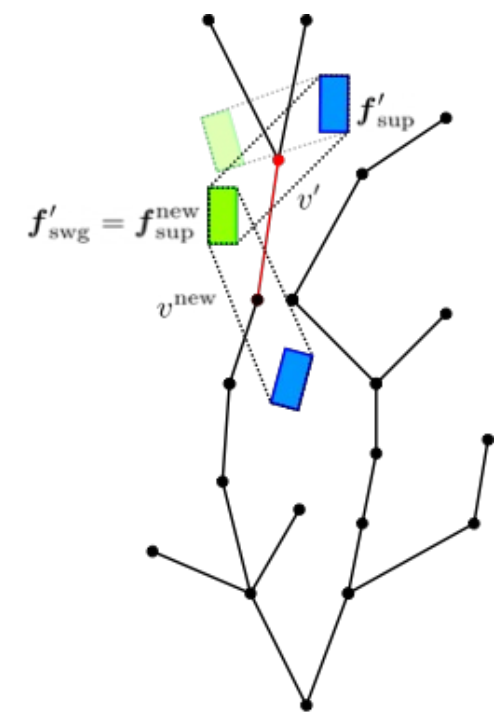
vertex selection



expansion



choose parent



rewire



# gait generation via IS-MPC: 3D motion model

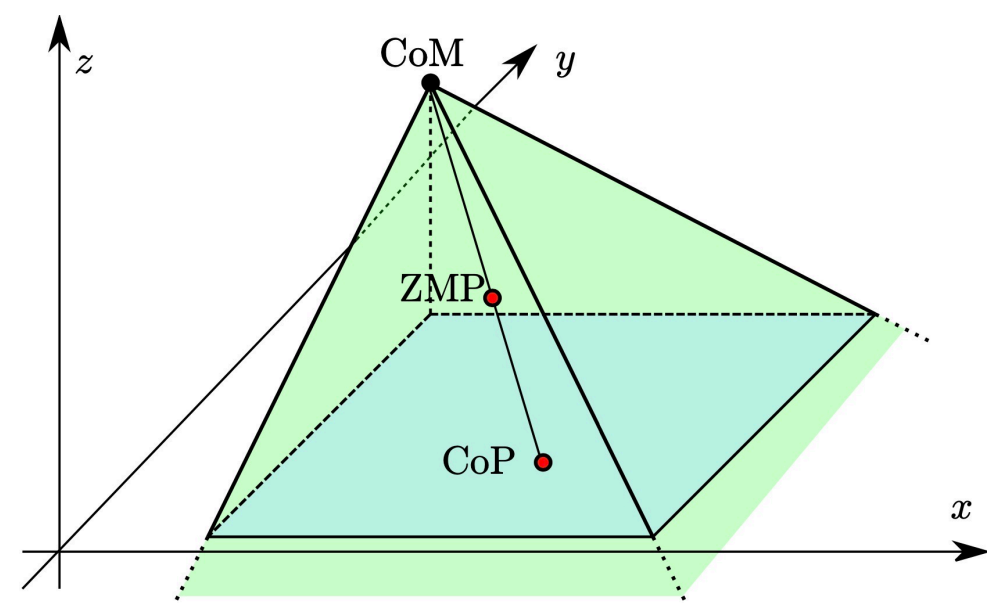
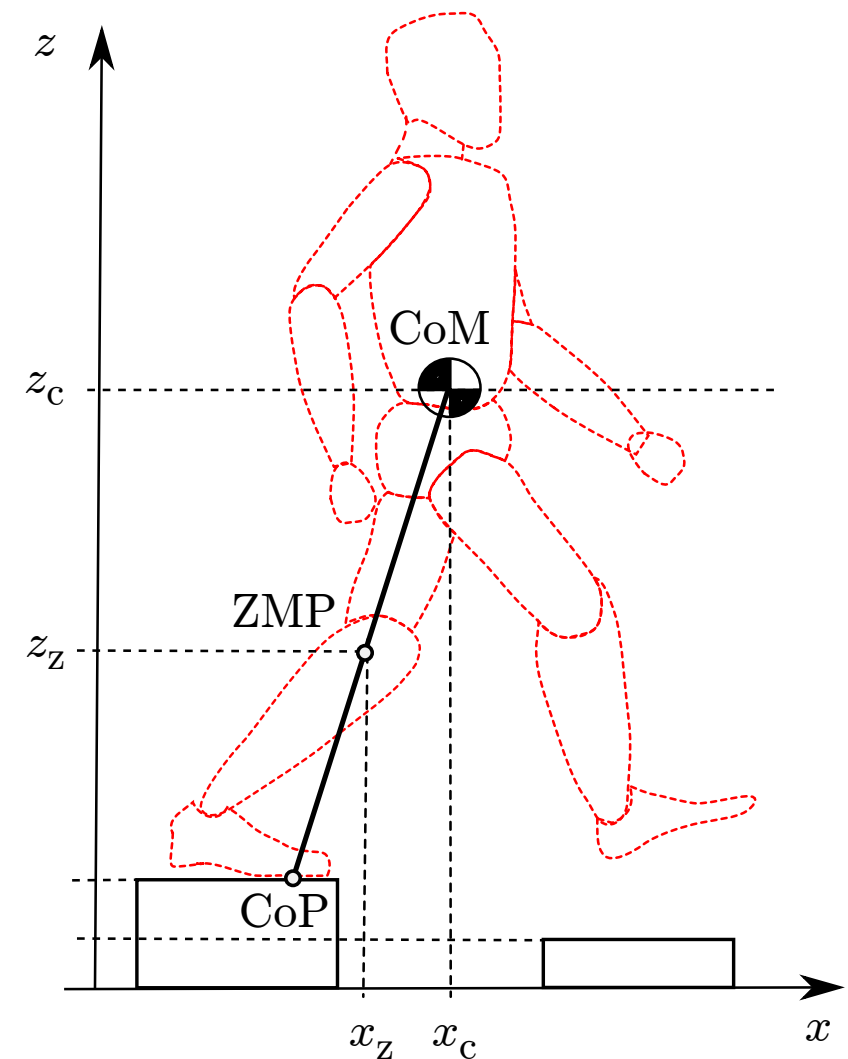
- LIPM not suitable for gait generation over uneven terrain due to constant height assumption
- linearity can be maintained by constraining vertical motion such that

$$\frac{\ddot{z}_c + g}{z_c - z_z} = \eta^2$$

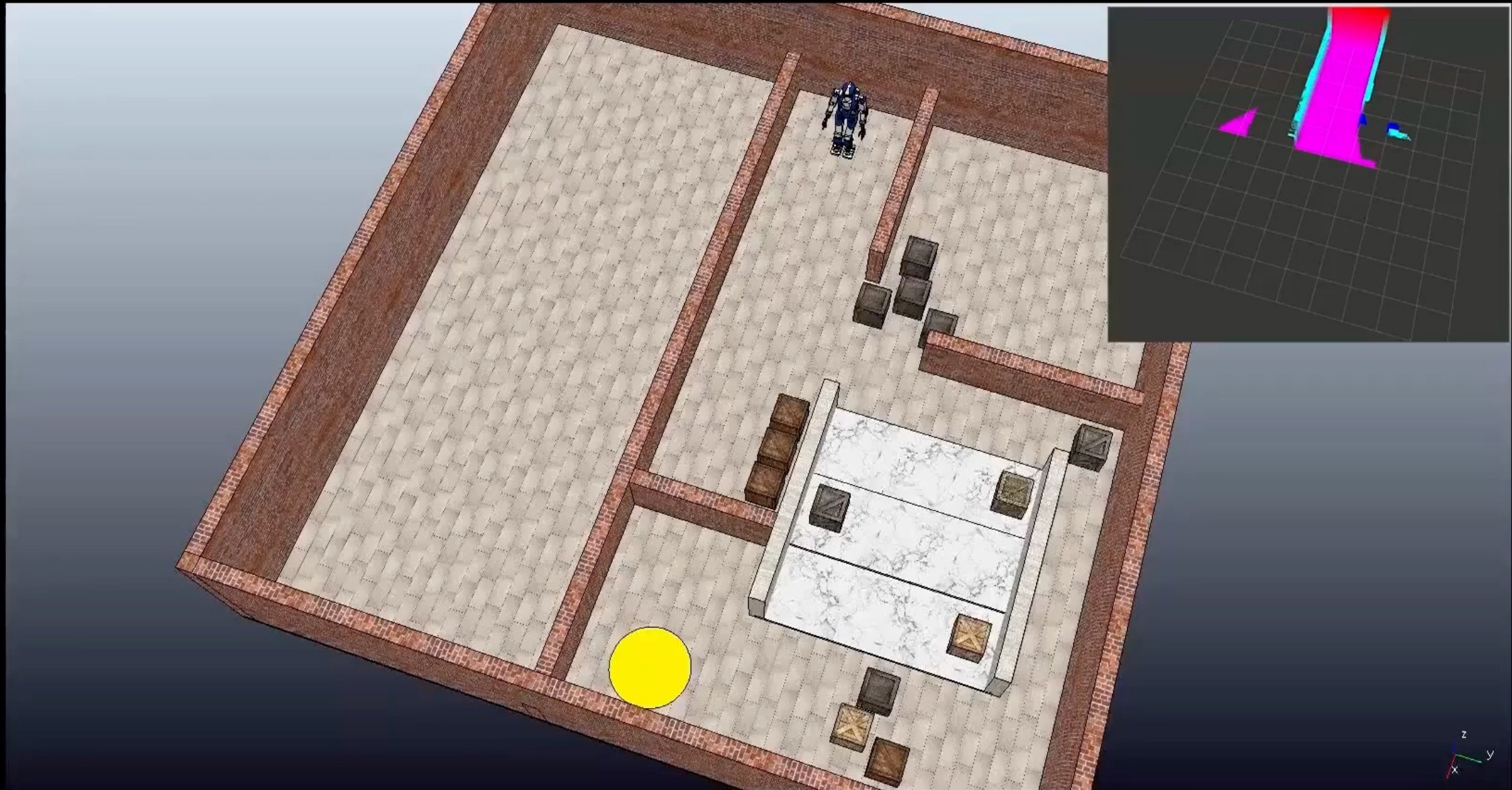
- CoM dynamics become

$$\ddot{p}_c = \eta^2(p_c - p_z) - g$$

- solve QP problem using MPC scheme



# V-REP simulations

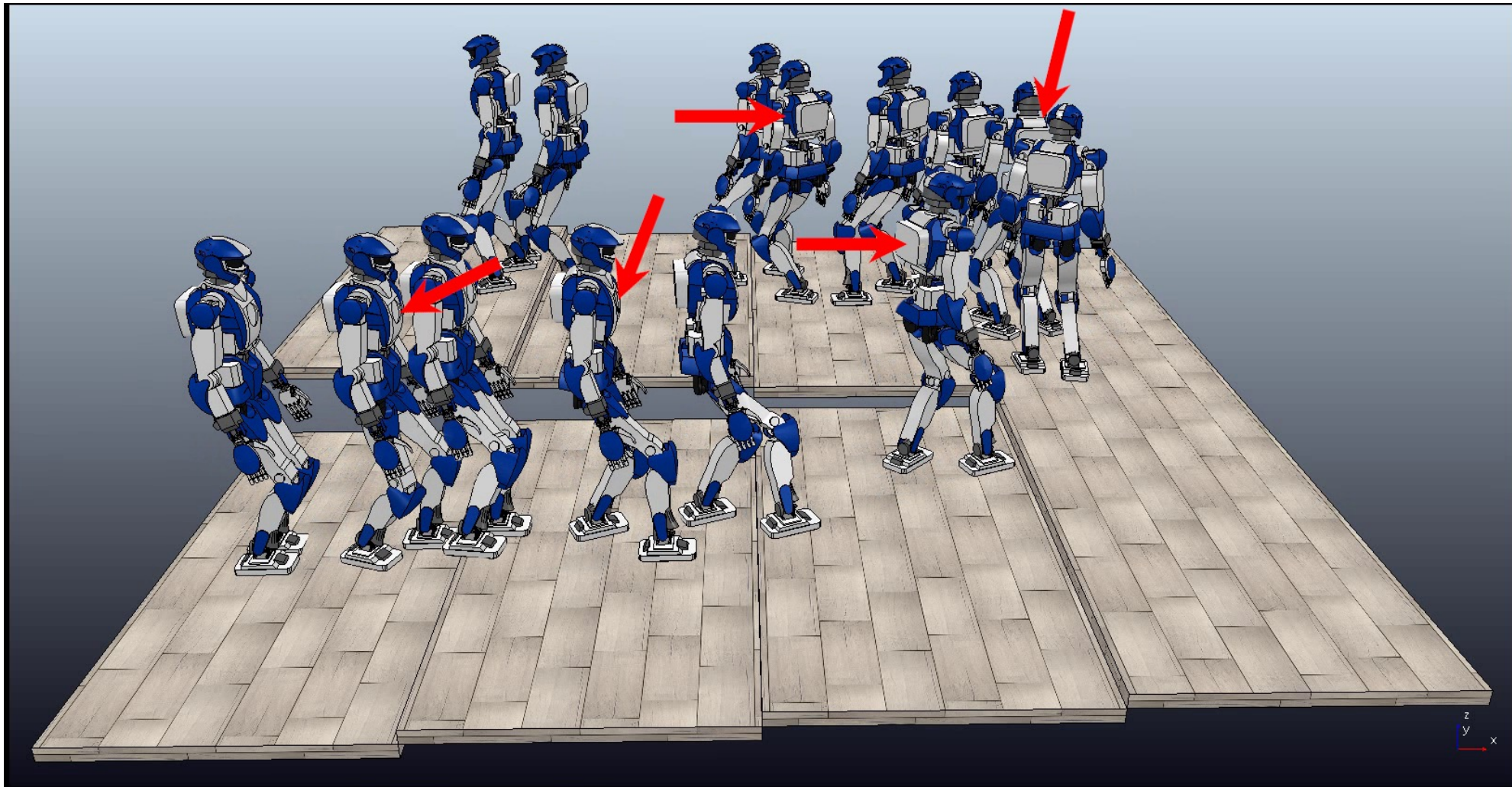


in the on-line case, the mapping module incrementally builds the elevation map using RGB-D images acquired by the humanoid while walking



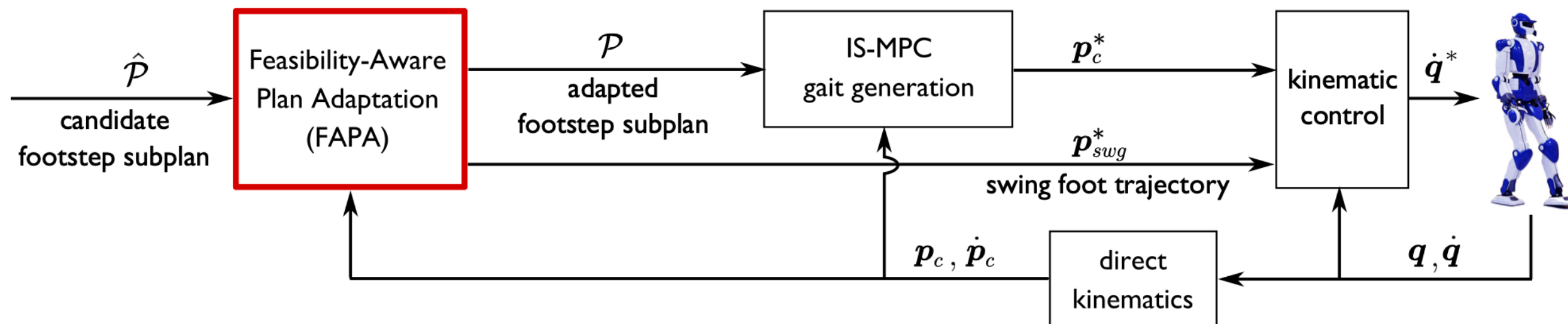
# feasibility-aware plan adaptation in humanoid gait generation

- **problem:** generate a feasible gait, even in case of **disturbances**
- it is assumed that the state of the robot is known



- **approach:** adapt **footstep plan** (positions, orientations and timings)

# architecture



- Feasibility-Aware Plan Adaptation (**FAPA**) module, it adapts the footstep plan before the IS-MPC stage
- being external to the MPC, it can enforce nonlinear constraints without a significant impact on the **performance** of the overall scheme

# FAPA module

- the adaptation is done in such a way to always make the IS-MPC stage **feasible** (i.e., able to satisfy balance and stability constraints)
- the feasibility of the MPC can be studied analytically and the resulting conditions constitute **gait feasibility constraints** in FAPA
- this ties the adaptation to the robot dynamics and makes it able to react to **pushes** and **disturbances**
- F-FAPA is an NLP and V-FAPA is a mixed-integer NLP

# FAPA module

- cost function minimizes displacement from the subplan subject to
  - a. kinematic constraints
  - b. timing constraints
  - c. fixed (F-FAPA) or variable (V-FAPA) patch constraints
  - d. current footsteps constraints
  - e. gait feasibility constraints
- the **gait feasibility constraints** ensure that the state is in the feasibility region of the IS-MPC

$$x_u^k + b_x^k \leq s^T Z^{-1} \left( MX_f^l + mx_f^l + z \left( \frac{d_x}{2} - x_z^k \right) \right)$$



## Feasibility-Aware Plan Adaptation in Humanoid Gait Generation

M. Cipriano, M. R. O. A. Maximo, N. Scianca, L. Lanari, G. Oriolo

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Sapienza Università di Roma

July 2023



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