A Concise Introduction to Automated Planning and PDDL

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Reasoning Robots: Reasoning about Action in Cognitive Robotics
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The challenge of building devices that act autonomously is at the center of the AI research from its origins.

At the center of the problem of autonomous behavior is the control problem (or action selection problem).

- specify a controller that selects the action to do next

Traditional hard-coded solutions specify a pre-scripted controller in a high-level language.

- They do not suffer combinatorial explosion.
- The burden is all put on the programmer.
- Hard-coded solutions are usually biased and tend to constraint the search in some way.

The question of action selection for AI researchers is:

- What is the best way to intelligently constrain this search?
Two approaches in AI to tackle autonomous behavior:

**Learning-based approach**
- The controller is *learnt from experience*.
  - Discovery and interpretation of meaningful patterns for a given task.
    - Learned solutions are usually black-box.

**Model-based approach**
- The controller is *derived automatically* from a model of the domain of interest, the actions, the current state, and the goal.
  - The models are all conceived to be general.
    - The problem of solving a model is computationally intractable.

In this lecture, we introduce the basic ingredients of automated planning and the PDDL language for representing planning problems.
In AI, **automated planning** is conceived as the:

*model-based approach for the automated synthesis of plans of actions to achieve goals.*
Planning Models

- **Several classes of planning models**, which depend on the properties of the problems to be represented:
  - full or partial observability of the current state;
  - uncertainty in the initial state (fully or partially known);
  - uncertainty in the actions dynamics (deterministic or not);
  - uncertainty represented by sets of states or probability distributions;
  - the type of feedback (full, partial or no state feedback).

...classical planners solve efficiently real problems with hundreds of propositions!

Planning is computationally intractable even for the simplest models...

..BUT..
Classical Planning Model

**finite** and **discrete** state space \( S \)

- **known initial state** \( I \in S \)

- a set \( S_G \subseteq S \) of **goal states**

- **actions** \( A(s) \subseteq A \) applicable in each \( s \in S \)

- a **deterministic transition function** \( s' = f(a,s) \) for \( a \in A(s) \)

- **positive action costs** \( c(a,s) \)

- A **solution** or **plan** is a sequence of applicable actions \( \pi = a_0, \ldots, a_n \) that maps \( I \) into \( S_G \)
  - There are states \( s_0, \ldots, s_{n+1} \) such that \( s_{i+1} = f(a_i, s_i) \) and \( a_i \in A(s_i) \) for \( i = 0, \ldots, n \) and \( s_{n+1} \in S_G \)

- A plan is **optimal** if it minimizes the sum of action costs \( \sum_{i=0}^{n} c(a_i, s_i) \). If costs are all 1, plan cost is plan length.
Example: The Blocks World Domain

- Given a set of blocks of various colors sitting on a table, the goal is to build one or more vertical stacks of these blocks.

- Initial state: \( I \)

- Goal: \( G \)

- Available actions: moving a block
  - from the table to the top of another block
  - from the top of another block to the table
  - from the top of one block to the top of another block
Planning Domain Definition Language

- The standard representation language for automated planners is known as the **Planning Domain Definition Language** (PDDL).

- Components of a PDDL planning task:
  - **Objects**: Things in the world that interest us.
  - **Predicates**: Properties of objects that we are interested in; they can be true or false.
  - **Initial state**: The state of the world that we start in.
  - **Goal specification**: Things that we want to be true.
  - **Actions/Operators**: Ways of changing the state of the world.
Problems in PDDL are expressed in two separate parts:

- PDDL **Planning Domain PD** (available actions and predicates representing explicit representation of the world).
- PDDL **Planning Problem PR** (objects, initial state $I$ and goal condition $G$).

- A planner that takes in input a problem encoded in PDDL is said to be **domain-independent**, since it is able to automatically produce a plan without knowing what the actions and domain stand for.
- PDDL provides the ground for performing a **direct comparison** between different planning techniques and algorithms and evaluating against classes of problems.
Domain files

Domain files look like this:

```
(define (domain <domain name>)
  <PDDL code for predicates>
  <PDDL code for first action>
  [...] 
  <PDDL code for last action>
)
```

- `<domain name>` is a string that identifies the planning domain, e.g., `blocks-world`.
- **Example on the web:** `blocks-world.pddl`
Problem files

- Problem files look like this:

```
(define (problem <problem name>))
 (:domain <domain name>)
 <PDDL code for objects>
 <PDDL code for initial state>
 <PDDL code for goal specification>
)
```

- `<problem name>` is a string that identifies the planning task, e.g. blocks-world-3.
- `<domain name>` must match the domain name in the corresponding domain file.
- Example on the web: blocks-world-3.pddl
Example: The Blocks World Domain

- **Objects**: The blocks locations. Blocks can be on the table or on top of another block. Four blocks for the specific instance.

- **Predicates**: Is a block clear (i.e., with no block on top)? Does a block have another block on top of it?

- **Actions/Operators**: Clear blocks can be moved on top of another block or on the table, respectively.

- **Initial state**: Blocks A, B and C are initial arranged on the table.

- **Goal specification**: re-arrange the blocks so that C is on A and A is on B.
(define (domain blocks-world)
 (:requirements :strips)
 (:objects block)
 (:predicates (on ?x ?y - block)
 (clear ?x - block)))

Objects of the domain and predicates describe the state of the world.
The Blocks World in PDDL
Planning Domain

(:action move
 :parameters (?b ?x ?y - block)
 :precondition (and (on ?b ?x)
                    (clear ?b) (clear ?y))
 :effect (and (not (on ?b ?x)) (not (clear ?y))
           (on ?b ?y) (clear ?x)))

Actions are described in terms of **preconditions** under which an action can be executed, and **effects** on the state of the world.

Both preconditions and effects are stated in terms of the predicates.
The Blocks World in PDDL
Planning Domain

(:action moveToTable
 :parameters (?b ?x - block)
 :precondition (and (on ?b ?x) (clear ?b))
 :effect (and (on ?b table) (clear ?x)
 (not (on ?b ?x)))
)
The Blocks World in PDDL
Planning Problem

Objects
(:objects A B C table - block)

Initial State I
(:init
 (on A table) (clear A)
 (on B table) (clear B)
 (on C table) (clear C))

Goal G
(:goal
 (and (on C A) (on A B))
)
Begin plan
1. (move A table B)
2. (move C table A)
End plan

Since $S_2$ is a state satisfying the goal $G$, the solution found is a valid plan.
The quality of a solution depends by the specific search algorithm employed by the planner.

Begin plan
1. (move B table A)
2. (move B A table)
3. (move A table B)
2. (move C table A)
End plan
Given $n$ blocks, the states include all the **n! possible towers of n blocks** plus additional combinations of lower towers.

For classical planning, the general problem of coming up with a plan is **PSPACE-complete**.

The size of the graph (i.e., the number of states) is **exponential** in the number of blocks.
Challenge of automated planning

- **Challenge**: achieving both **generality** and **scalability**.
  - **Generality**: A planner can solve *arbitrary problem instances*.
    - A planner does not know what the actions, and domain stand for.
    - This is very different from writing a *domain-specific* solver.
  - **Scalability**: Planners embed very effective **domain-independent heuristics** to drive the searching task towards the goal.
    - An *heuristic function* provides an estimate of the cost to reach the goal from the current state (Examples: Best-First Search, A*, Hill Climbing, etc).
  - State-of-the art planners** provide **customized implementations** of the search algorithms with different properties of completeness, optimality, and memory complexity.

Several extensions of PDDL:

- **PDDL 1.2**: Base version of the language. Among the basic constructs, it includes STRIPS, ADL and conditional effects.

- **PDDL 2.1**: It introduces numeric fluents (e.g., to model non-binary resources such as time, distance, weight, etc.), plan-metrics (to allow quantitative evaluation of plans, and not just goal-driven), and durative/continuous actions (which could have variable, non-discrete length, conditions and effects).

- **PDDL 2.2**: It introduces derived predicates (to model the dependency of given facts from other facts), and timed initial literals (to model exogenous events occurring independently from plan-execution).

- **PDDL 3.0**: It introduces preferences (hard- and soft-constraints, in form of logical expressions, to be satisfied in specific points of the plan).

- **PDDL 3.1**: It introduces object fluents (functions' range can be any object-type).
Notes on action effects

- In the base version of PDDL (v1.2), action effects can be more complicated than seen so far.

- They can be **universally quantified**:
  \[
  \text{(forall (v_1 \ldots v_n))}
  \text{<effects>}
  \]

- They can be **conditional**:
  \[
  \text{(when <condition>}
  \text{<effect>)}
  \]

- We now investigate a **concrete problem** *(trace alignment in process mining)* solved by planning techniques that require the use of conditional effects and universal quantification in actions effect.
The Blocks World in PDDL

Conditional effects

(:action move
 :parameters (?b ?x ?y - block)
 :precondition (and (on ?b ?x) (clear ?b))
 :effect (and (not (on ?b ?x)) (clear ?x))
  (when (clear ?y)
   (and (on ?b ?y) (not (clear ?y))))
  (when (not (clear ?y))
   (on ?b table))
)

Using conditional effects allows to model a single planning action that represent blocks movement.
Any execution of a process model produces a new execution trace (i.e., a process instance) recorded in an event log.

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The trace alignment problem

- Process models are typically not enforced by information systems (human behavior is often involved).
  - Traces can be dirty, with spurious or missing events.

- **Trace alignment** is the problem of cleaning such dirty traces against process models to the aim of:
  - verify if a trace is compliant with its underlying process model;
  - identifying the root and the severity of each deviation;
  - repairing the trace to make it compliant with the process model.

- The existing techniques to compute optimal alignments
  - provide ad-hoc implementations of the A* algorithm.
  - do not scale efficiently when process models and event logs are of considerable size.

**SOLUTION**: The problem of computing optimal alignments can be formulated as a planning problem in PDDL, which employs conditional effects and universal quantifiers.
Trace alignment

- Given a trace $t$ and a DECLARE model $D$ (which is used to define the regulations) find the optimal alignment of $t$ with respect to $D$.
  - A DECLARE model $D = (A, \pi_D)$ consists of a set of activities $A$ involved in a process and a collection of **temporal constraints** $\pi_D$ defined over $A$.
  - DECLARE constraints (aka **templates**) define parameterized classes of properties and enjoy a precise semantics in $\text{LTL}_f$ (LTL over finite traces).

**Existence($A$)**
- LTL Formalization: $\Diamond A$
- $A$ occurs at least 1 time.
- $BCAAC \checkmark$, $BCC \times$

**Absence($C$)**
- LTL Formalization: $\neg \Diamond C$
- $A$ never occur.
- $BAA \checkmark$, $BCAC \times$

**Response($A$, $B$)**
- LTL Formalization: $\square (A \rightarrow \Diamond B)$
- If $A$ occurs, then $B$ occurs after $A$.
- $BCAAC \times$, $CAACB \checkmark$, $BCC \checkmark$
From LTL$^f$ to DFAs

- For any LTL$^f$ formula there exists a DFA that accepts all the traces satisfying the formula.

**Existence** ($A$)
LTL Formalization: ◊$A$
A occurs at least 1 time.
$BCAAC \checkmark \ BCC \times$

**Absence** ($C$)
LTL Formalization: $\neg$◊$C$
A never occur.
$BAA \checkmark \ BCAC \times$

**Response** ($A, B$)
LTL Formalization: $\Box (A \rightarrow \Diamond B)$
If A occurs, then B occurs after A.
$BCAAC \times \ CAACB \checkmark \ BCC \checkmark$
Automata-based solution

- Trace alignment can be solved using automata:
  - One automaton for the trace (\textit{trace automaton}).

- Accepts input trace \(<C,B/>\) plus all other traces, however…
- …changes wrt. input trace must be marked by \textit{add/del}, e.g.,
  - \(<C,B,C/> = C B \text{ addC}\)
  - \(<B,C,B,B/> = \text{delC} B \text{ addC addB addB}\)
- \textit{Adds} and \textit{dels} have (possibly different) positive costs.
Automata-based solution

- One automaton per constraint (*constraint automaton*) augmented to account for *adds* and *dels*.

- Accepts all (possibly repaired) traces satisfying the constraint.

- An *alignment* is a sequence of **synchronous steps** performed in all *augmented constraint automata* and in the *augmented trace automaton* such that -- at the end of the alignment -- each automaton is **in at least one** accepting state.
An example of Trace Alignment

**Trace:** <C, B>

**LTL Constraints**

**Existence(A):** ◊A

**Absence(C):** ¬◊C

**Response(A,B):** □(A → ◊B)
An example of Trace Alignment

Trace: \( <C, B> \)

LTL\(_f\) Constraints

Existence(A): \( \Diamond A \)

Absence(C): \( \neg \Diamond C \)

Response(A,B): \( \Box (A \rightarrow \Diamond B) \)

Augmented trace automaton and augmented constraint automata
An example of Trace Alignment

Trace: \langle C, B \rangle

Optimal Plan: \langle delC, addA, B \rangle

LTL\textsubscript{f} Constraints

Existence(A): \diamond A

Absence(C): \neg \diamond C

Response(A,B): \square (A \rightarrow \diamond B)

...if adds and dels have unitary cost.
The automata-based approach can be recast as a **cost-optimal planning problem** using PDDL.

**Planning Domain:**
- Input events modeled by *synchronization actions* with null cost.
- *Adds* and *dels* modeled by planning actions with positive costs.
- **Domain propositions** encode the structure and the dynamics of the augmented trace and of all augmented constraint automata.

**Problem:**
- **Initial state**: all automata in their starting state.
- **Goal state**: all automata in (at least one) final state.

**Solution:**
- **Optimal** (i.e., minimal-cost) plan to reach the goal state.
PDDL Planning Domain

Boolean Predicates

(types trace_state automaton_state - state activity)

It captures the activities involved in a transition between two states of a constraint/trace automaton.

They identify the states of any constraint automaton and of the trace automaton.

(:predicates

(trace ?t1 - trace_state
   ?e - activity
   ?t2 - trace_state)
(automaton ?s1 - automaton_state
   ?e - activity
   ?s2 - automaton_state)
(cur state ?s - state)
(final state ?s - state)
)

They hold if there exists a transition in the trace/constraint automaton from two states, being \( e \) the activity involved in the transition.

They hold if \( s \) is the current/accepting state of a trace/constraint automaton.
 (:action sync
  :parameters (?t1 - trace_state ?e - activity ?t2 - trace_state)
  :precondition (and (cur_state ?t1) (trace ?t1 ?e ?t2))
  :effect (and (not (cur_state ?t1)) (cur_state ?t2)
    (forall (?s1 ?s2 - automaton_state)
      (when (and (cur_state ?s1)
        (automaton ?s1 ?e ?s2))
      (and (not (cur_state ?s1))
        (cur_state ?s2))))))

It is applied only if there exists a transition from the current state \( t_1 \) of the trace automaton to a subsequent state \( t_2 \), being \( e \) the activity involved in the transition. The action **has no cost**, as it stands for no change in the trace.

**CONDITIONAL EFFECT**: The action is performed in each constraint automaton for which there exists a transition involving the activity \( e \) that connects \( s_1 \) – the current state of the automaton – with a different state \( s_2 \).
PDDL Planning Domain

Add action

(:action add
  :parameters (?e - activity)
  :effect (and (increase (total-cost) 1)
    (forall (?s1 ?s2 - automaton_state)
      (when (and (cur_state ?s1)
        (automaton ?s1 ?e ?s2))
        (and (not (cur_state ?s1))
          (cur_state ?s2)))))))

CONDITIONAL EFFECT: The action is performed only for transitions involving the activity e between two different states of any constraint automaton, with the current state of the trace automaton that remains the same after the execution of the action.
PDDL Planning Domain

*Del action*

Del actions make total cost of the alignment increasing of a predefined value.

```pddl
(:action del
 :parameters (?t1 - trace_state ?e - activity ?t2 - trace_state)
 :precondition (and (cur_state ?t1) (trace ?t1 ?e ?t2))
 :effect(and (increase (total-cost) 1)
            (not (cur_state ?t1)) (cur_state ?t2)))
```

It yields a single move in the trace automaton.
(:objects
  t0 t1 t2 - trace_state
  s4 s5 - automaton_state
  A B - activity)

(:init
  (= (total-cost) 0)

(cur_state t0)
(trace t0 C t1)
(trace t1 B t2)
(final_state t2)

(cur_state s4)
(automaton s4 A s5)
(automaton s5 B s4)
(final_state s5))

(:goal (forall (?s - state)
  (imply (cur_state ?s)(final_state ?s))))

(:metric minimize (total-cost))
Concluding Remarks

- Planning models are **all general** in the sense that they are **not bound** to specific problems or domains.

- This **generality** is coupled with the notion of **intelligence** which requires the ability to deal with new problems.

- The price for generality is **computational**:
  - planning over models represented in compact form is **intractable** in the worst case, yet currently large classical problems can be solved **very quickly**.

**Suggested reading and resources**