

Optimal design of electric motors



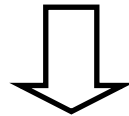
7.5 kW, 380 V, 50 Hz, 4 poles, three-phase

Optimal design of electric motors

Electric motors are widely used in industrial and domestic applications

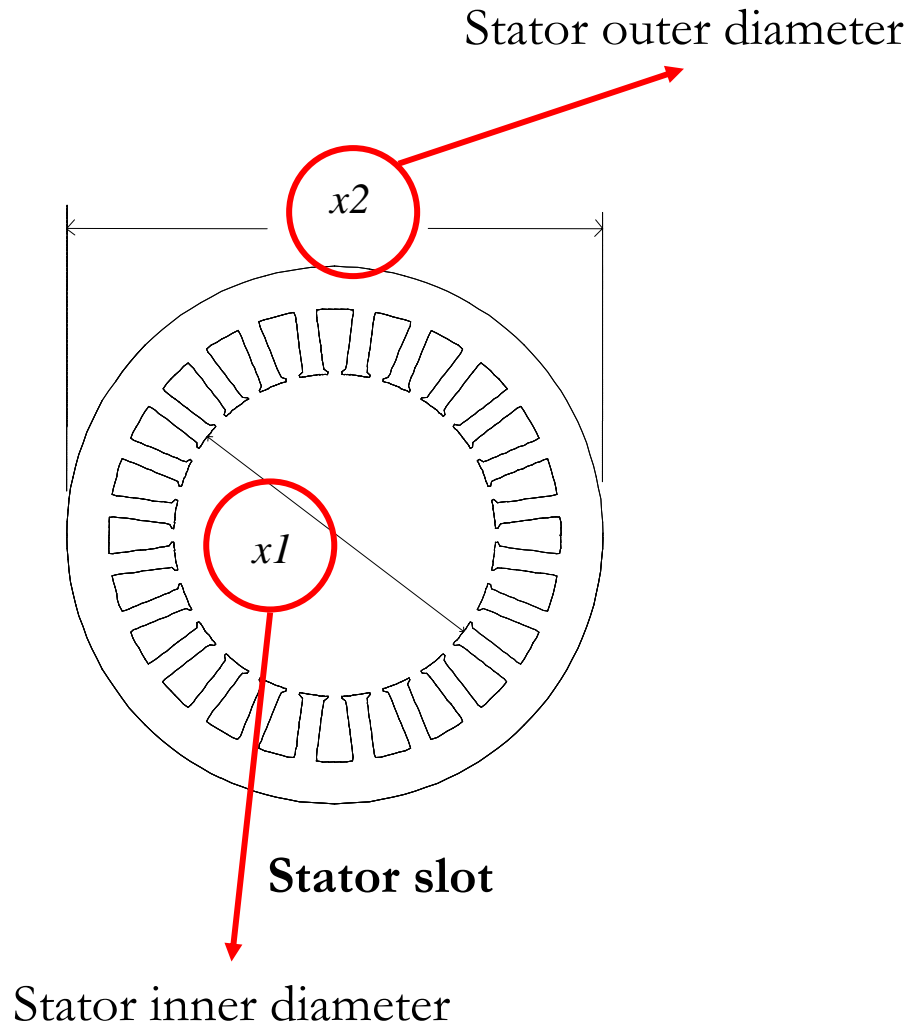
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Optimized design can improve the efficiency of the motors

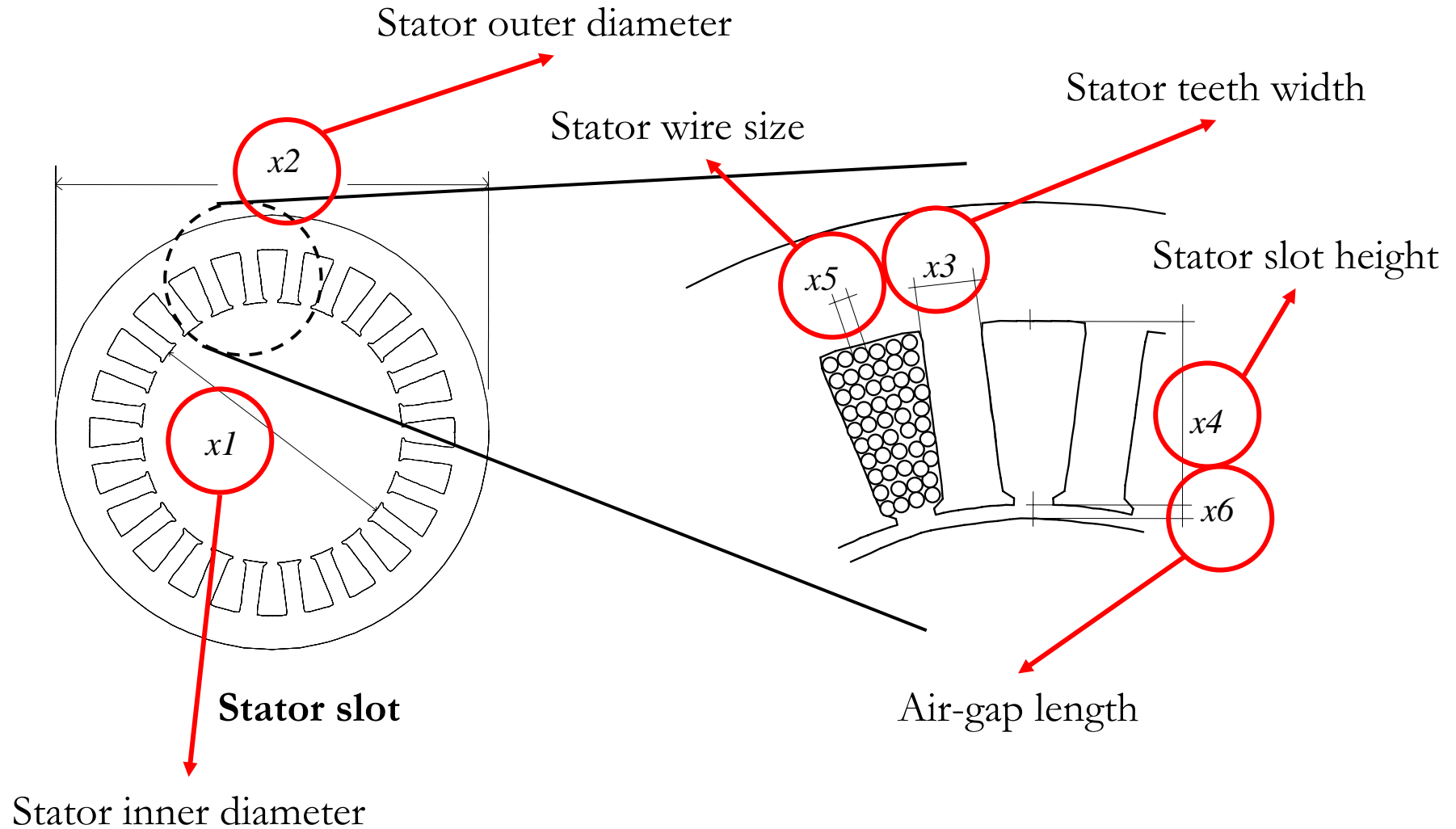


Reduction of energy consumption

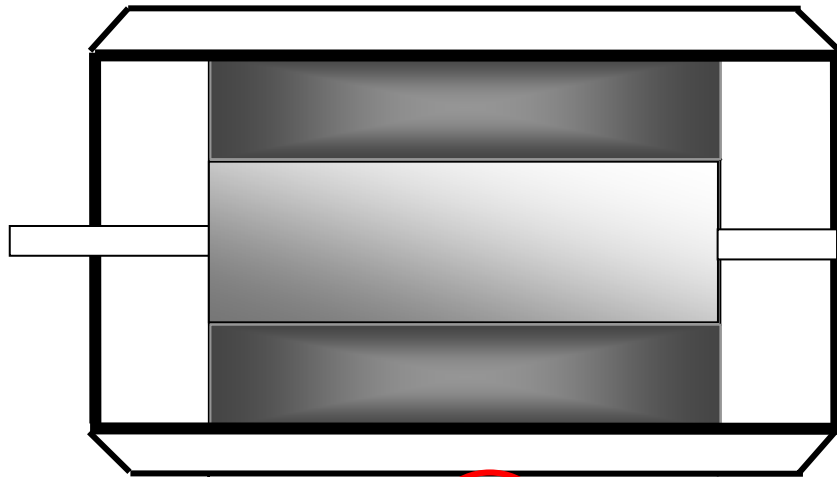
Independent Variables – Design Parameters



Independent Variables – Design Parameters

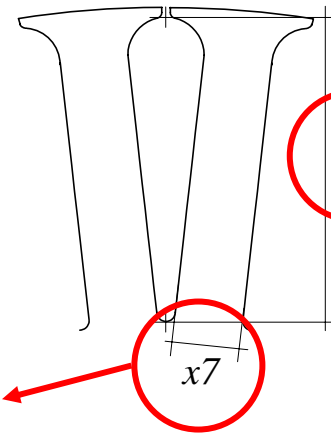


Independent Variables – Design Parameters



x_9

Stack length



Rotor slot height :

x_8

Rotor teeth width

x_7

Rotor slot

Independent Variables – Design Parameters

Stator inner diameter : $120.0mm \leq x_1 \leq 130.0mm$

Stator outer diameter : $180mm \leq x_2 \leq 220mm$

Stator teeth width : $4.5mm \leq x_3 \leq 6.5mm$

Stator slot height : $16mm \leq x_4 \leq 19mm$

Stator wire size : $1.4mm^2 \leq x_5 \leq 4.0mm^2$

Air-gap length : $0.3mm \leq x_6 \leq 0.5mm$

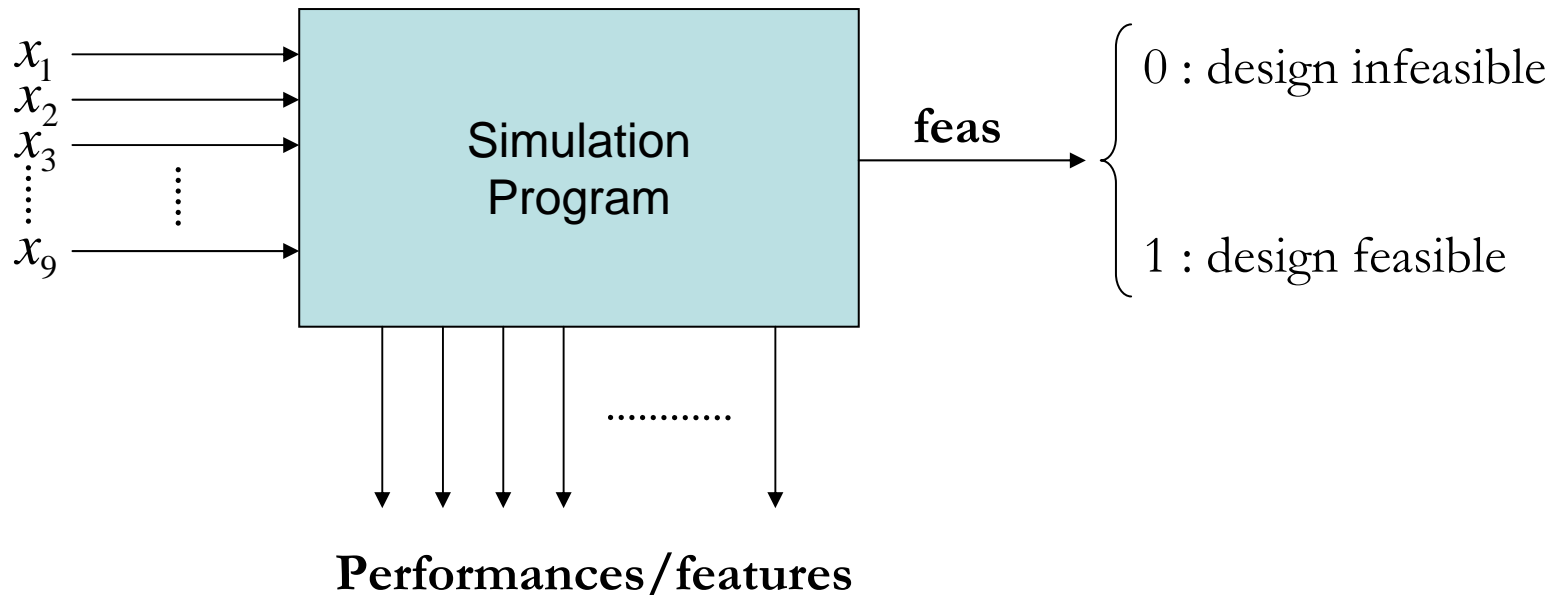
Rotor teeth width : $3.5mm \leq x_7 \leq 5mm$

Rotor slot height : $16mm \leq x_8 \leq 18.5mm$

Stack length : $140mm \leq x_9 \leq 190mm$



Simulation and Performance Evaluation



Manufacturing cost

Operating cost

Rated efficiency

Rated power

Power factor at rated load

Starting current

Starting torque

Breakdown torque

Stator slot fullness

Stator winding temperature

Rotor bars temperature

Induction in the stator and rotor teeth

Rated slip

Nonlinear Constraints

Rated power: $p_{wi} \leq 7560W$

Power factor at rated load: $\cos \varphi \geq 0.8$

Starting current: $I_{st} \leq 67A$

Starting torque: $T_{st} \geq 97Nm$

Breakdown torque: $T_{max} \geq 140Nm$

Stator slot fullness: $k_{ssf} \leq 0.55$

Stator winding temperature: $T_{cu} \leq 130^{\circ}C$

Rotor bars temperature: $T_{al} \leq 150^{\circ}C$

Induction in the stator teeth: $1.2T \leq H_{st} \leq 1.8T$

Induction in the rotor teeth: $1.2T \leq H_{rt} \leq 1.8T$

Rated slip: $RS \leq 0.05$



Initial Feasible Design

Existing motor having
a Rated Efficiency of 88.38%

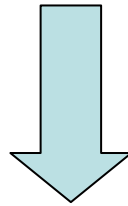
(Real Measured Efficiency of 84.2%)

$$\left\{ \begin{array}{l} x_1 = 126.6mm \\ x_2 = 200mm \\ x_3 = 5.5mm \\ x_4 = 17.5mm \\ x_5 = 1.5727mm^2 \\ x_6 = 0.4mm \\ x_7 = 4mm \\ x_8 = 17.8mm \\ x_9 = 160mm \end{array} \right.$$

Problem Statement

find x^* such that $f(x^*) \leq f(x)$

for all $x \in \{x : l \leq x \leq u, g(x) \leq 0\}$



$\arg \min f(x)$

s.t. $g(x) \leq 0$

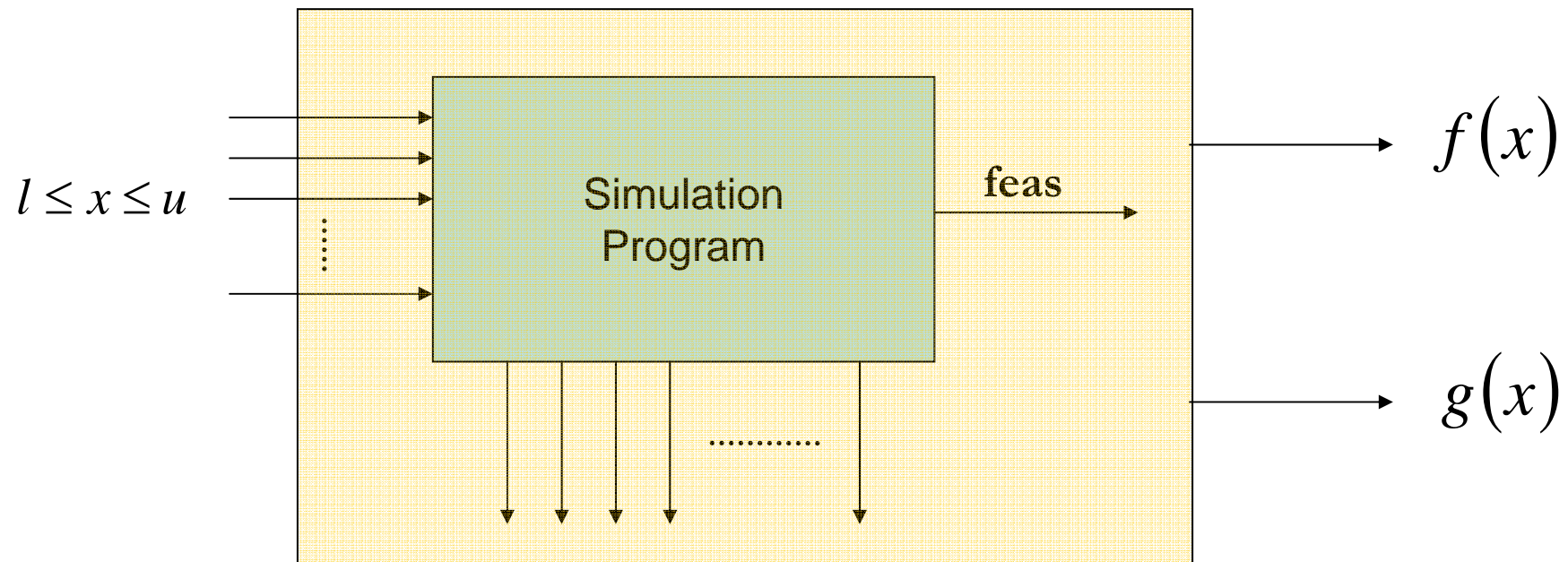
$l \leq x \leq u$

Problem Statement

$$\arg \min f(x)$$

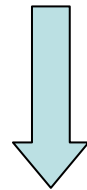
$$\text{s.t. } g(x) \leq 0$$

$$l \leq x \leq u$$



Problem Properties

- Nonlinear objective and constraints
- Analytical expression of $f(x)$ and $g(x)$ not available:
No Derivative Knowledge
- Presence of so-called hidden constraints
- Computation of $f(x)$ and $g(x)$ affected by numerical errors



A difficult Global Optimization problem

Induction Motor Optimal Design

“optimal” design:

(initial design:)

Stator inner diameter :	$x_1 = 129.94mm$	(126.6mm)
Stator outer diameter :	$x_2 = 220mm$	(200mm)
Stator teeth width :	$x_3 = 4.53mm$	(5.5mm)
Stator slot height :	$x_4 = 19mm$	(17.5mm)
Stator wire size :	$x_5 = 2.635mm^2$	(1.573mm ²)
Air-gap length :	$x_6 = 0.3mm$	(0.4mm)
Rotor teeth width :	$x_7 = 3.543mm$	(4mm)
Rotor slot height :	$x_8 = 18.5mm$	(17.8mm)
Stack length :	$x_9 = 187.1mm$	(160mm)



Optimized design



Induction Motor Optimal Design

“optimal” design:

initial design:

Rated Efficiency of 91.9%

Rated Efficiency of 88.38

Real Measured Efficiency 90.2% **Real Measured Efficiency 84.2%**



Optimal design of electric motors

Associazione Nazionale Industrie Elettromeccaniche

il parco motori nazionale relativo alla taglia da 7.5 kW - 4 poli
si aggira intorno ai 30000 motori
(per usi industriali: nastri trasportatori, ventilatori,...)

l'uso dei motori ottimizzati implicherebbe un risparmio annuo di
35 GWh/anno pari a circa 3.5 Milioni di €/anno

