Exercise 1
Given the following \( \mathcal{ALC} \) TBox:

\[
\begin{align*}
A & \sqsubseteq B \\
A & \sqsubseteq C \\
B & \sqsubseteq \forall R.D \\
C & \sqsubseteq \forall R.E \\
D & \sqsubseteq \neg E
\end{align*}
\]

(a) tell whether the TBox \( \mathcal{T} \) is satisfiable, and if so, show a model for \( \mathcal{T} \);

(b) tell whether the concept \( A \) is satisfiable with respect to \( \mathcal{T} \), and if so, show a model for \( \mathcal{T} \) where the interpretation of \( A \) is non-empty;

(c) given the ABox \( A = \{ A(a) \} \), tell whether the knowledge base \( \langle \mathcal{T}, A \rangle \) is satisfiable (consistent), explaining your answer.

Exercise 2
Given the following ASP program \( P \):

\[
\begin{align*}
r(x,y) :& \leftarrow p(x,y). \\
r(x,y) :& \leftarrow p(x,z), r(z,y). \\
s(x,y) :& \leftarrow q(x,y). \\
s(x,y) :& \leftarrow r(x,y). \\
s(x,y) :& \leftarrow q(x,z), s(z,y). \\
t(x,y) :& \leftarrow s(x,y), \neg r(x,y). \\
p(a,b). \quad p(b,c). \quad q(c,d). \quad q(d,e).
\end{align*}
\]

(a) tell whether \( P \) is stratified;

(b) compute the answer sets of \( P \).

Exercise 3
We want to formalize knowledge about the domain of movies. In particular, we want to formalize the following statements:

1. every director is a person;
2. every actor is a person;
3. every movie has (at least) a director;
4. property “is director of” has domain director and range movie;
5. property “acts in” is a subproperty of property “works in”;
6. actor and movie are disjoint classes;

(a) Choose the most appropriate knowledge representation language for expressing the above knowledge among the following: \( \mathcal{ALC} \), Datalog, ASP, OWL, DL-Lite, RDFS;

(b) express the above knowledge in the formalism chosen at the previous point.

Exercise 4
(a) Write an RDF/RDFS model representing the following statements about URIs Person, Director, Actor, Country, Movie, filmedIn, isDirectorOf, actsIn, bornIn, Jane, Joe, Mary, Paul, Italy, ABC, XYZ.

1. Person, Director, Actor, Country and Movie are classes;
2. Director and Actor are subclasses of Person;
3. actsIn, bornIn, filmedIn and isDirectorOf are properties;
4. isDirectorOf has domain Director and range Movie;
5. filmedIn has domain Movie and range Country;
6. bornIn has domain Person and range Country;
7. actsIn has domain Actor and range Movie;
8. Jane is the director of movie XYZ;
9. Paul and Mary act in movie ABC;
10. ABC was filmed in Italy;
11. Joe is a director.
(b) Write SPARQL queries corresponding to the following requests: (b1) “return all directors of movies filmed in Italy”; (b2) “return every movie that was filmed in the same country where the director was born in”.

Exercise 5
(a) Write an OWL ontology that formalizes the domain described at point (a) of Exercise 4.
(b) Add to the above ontology the axioms formalizing the following statements:

1. add the new classes EuropeanCountry and EuropeanMovie and state that EuropeanMovie corresponds to the class of movies filmed in European countries;
2. add a new property isDirectedBy and state that it is the inverse of isDirectorOf;
3. every movie is directed by at least one director;
4. every movie is filmed in at least one country;
5. Country and Movie are disjoint classes;
6. bornIn and actsIn are disjoint properties;

Then, tell whether the resulting OWL ontology is redundant, i.e.: can some of the axioms constituting the ontology be deleted without changing the meaning (that is, the models) of the ontology? if so, identify and list such axioms.

Exercise 6
(a) Axiomatize the following scenario, appropriately with action precondition and effect axioms, and obtain successor state axioms.

   - doorOpen(s) - The door is open in situation s.
   - insideRoom(s) - The robot is inside the room in situation s.

Actions:

- openDoor - The robot opens the door. This can be done if the robot is not inside the room and the door is closed (that is, not open), and has the effect that the door will be open.
- closeDoor - The robot closes the door. This can be done if the robot is inside the room and the door is open, and has the effect that the door will be closed.
- enter - The robot enters the room. This requires that the door is open and the robot is not inside the room, and has the effect that the robot will be inside the room.

Initial situation description: Initially the robot is not inside the room and the door is closed (that is, not open).

(b) Show, by applying regression, that the robot will be inside the room after the sequence of actions openDoor, enter, closeDoor, and that the sequence of actions is indeed executable.